1st Science Physics Laboratory Manual

PHYC 10150 Physics for Engineers 1 2017-2018



| Name |
|-----------------|
| Partner's Name |
| Demonstrator |
| Group |
| Laboratory Time |

Contents

| | Introduction | 3 |
|--------------|--------------------------------------|----|
| | Laboratory Schedule | 4 |
| | Grading Process and Lab Rules | 5 |
| | UCD plagiarism statement | 6 |
| Experiments: | Springs | 7 |
| | Investigating the Behaviour of Gases | 15 |
| | Conservation of Momentum | 25 |
| | Investigation of Electric Circuits 1 | 35 |
| | Investigation of Acceleration | 53 |
| | Investigation of Electric Circuits 2 | 65 |
| | Investigation of Rotational Motion | 77 |
| | Graphing | 87 |

Introduction

Physics is an experimental science. The theory that is presented in lectures has its origins in, and is validated by, experiment.

Laboratories are staged through the semester in parallel to the lectures. They serve a number of purposes:

- an opportunity, as a scientist, to test theories by conducting meaningful scientific experiments;
- a means to enrich and deepen understanding of physical concepts presented in lectures;
- an opportunity to develop experimental techniques, in particular skills of data analysis, the understanding of experimental uncertainty, and the development of graphical visualisation of data.

Based on these skills, you are expected to present experimental results in a logical fashion (graphically and in calculations), to use units correctly and consistently, and to plot graphs with appropriate axis labels and scales. You will have to draw clear conclusions (as briefly as possible) from the experimental investigations, on what are the major findings of each experiment and whetever or not they are consistent with your predictions. You should also demonstrate an appreciation of the concept of experimental uncertainty and estimate its impact on the final result.

Some of the experiments in the manual may appear similar to those at school, but the emphasis and expectations are likely to be different. Do not treat this manual as a 'cooking recipe' where you follow a prescription. Instead, understand what it is you are doing, why you are asked to plot certain quantities, and how experimental uncertainties affect your results. It is more important *to understand and show your understanding* in the write-ups than it is to rush through each experiment ticking the boxes.

This manual includes blanks for entering most of your observations. Additional space is included at the end of each experiment for other relevant information. All data, observations and conclusions should be entered in this manual. Graphs may be produced by hand or electronically (details of a simple computer package are provided) and should be secured to this manual.

There will be six 2-hour practical laboratories in this module evaluated by continual assessment. Note that each laboratory is worth 5% so each laboratory session makes a significant contribution to your final mark for the module. Consequently, attendance and application during the laboratories are of the utmost importance. At the end of each laboratory session, your demonstrator will collect your work and mark it.

Laboratory Schedule

Depending on your timetable, you will attend on even weeks on either Monday Wednesday or Friday from 11am to 1pm or on Monday afternoon from 4pm until 6pm. Groups scheduled for a Monday will have a lab in week 7 rather than week 8, which is a bank holiday. The class is divided into groups, numbered 1-10 in the table below.

Please consult the lab notice board or contact the lab manager, Thomas O'Reilly (Room Science East 1.41) to see which of the experiments you will be performing each week. This information is also summarized below.

| Semester | | Room | |
|----------|----------------------|------------------|----------------------|
| Week | Science East 143 | Science East 144 | Science East 145 |
| 2 | Springs: | Springs: | Springs: |
| | 1,4,7,10 | 3,6,9 | 2,5,8,11 |
| 4 | Gas: | Momentum: | Electric Circuits: |
| | 2,5,8,11 | 1,4,7,10 | 3,6,9 |
| 6 | Gas: | Momentum: | Electric Circuits: |
| | 3,6,9 | 2,5,8,11 | 1,4,7,10 |
| 7 | Gas: | Momentum: | Electric Circuits: |
| | 1,10 | 3 | 2,11 |
| 8 | Gas: | Momentum: | Electric Circuits: |
| | 4,7 | 6,9 | 5,8 |
| 10 | Electric Circuits 2: | Newton 2: | Electric Circuits 2: |
| | 2,5,8,11 | 1,4,7,10 | 3,6,9 |
| 12 | Rotation: | Newton 2: | Electric Circuits 2: |
| | 3,6,9 | 2,5,8,11 | 1,4,7,10 |

Grading Process

Grading is an important feedback for students and as such this is staged through the semester in close synchronisation with the labs. Students benefit from this feedback for continuous improvement through the semester. This is the grading process:

- 1. A lab script is graded and returned to the student in the subsequent scheduled lab slot.
- 2. Students resolve concerns regarding their grade with the demonstrator either during or immediately after this lab slot.
- 3. Grades are preliminary but can be expected to count towards a module grade once visible online. A grade is visible online within two weeks of the graded script being returned.

If the above doesn't happen, it is the student responsibility to resolve this with the demonstrator as early as possible.

Lab Rules

- 1. No eating or drinking
- 2. Bags and belongings should be placed on the shelves provided in the labs
- 3. Students must have their lab manual with them and bring any completed pre-lab assignments to the lab
- 4. It is the student's responsibility to attend an originally assigned lab slot. Zero grade is assigned by default for no attendance at this lab.

In the case of unavoidable absence, it is the student's responsibility to complete the lab in an alternative slot as soon as possible. The student is graded if doing so, however such a slot can't be guaranteed as lab numbers are strictly limited. The lab manager, Thomas O'Reilly (Room Science East 1.41), may be of help in discussing potential alternative lab times. Where best efforts have been made to attend an alternative but this still hasn't been possible, students should then discuss with their module coordinator.

5. Students work in pairs in the lab, however students are reminded that reports should be prepared individually and should comply with UCD plagiarism policy (see next page).

UCD Plagiarism Statement

(taken from http://www.ucd.ie/registry/academicsecretariat/docs/plagiarism_po.pdf)

The creation of knowledge and wider understanding in all academic disciplines depends on building from existing sources of knowledge. The University upholds the principle of academic integrity, whereby appropriate acknowledgement is given to the contributions of others in any work, through appropriate internal citations and references. Students should be aware that good referencing is integral to the study of any subject and part of good academic practice.

The University understands plagiarism to be the inclusion of another person's writings or ideas or works, in any formally presented work (including essays, theses, projects, laboratory reports, examinations, oral, poster or slide presentations) which form part of the assessment requirements for a module or programme of study, without due acknowledgement either wholly or in part of the original source of the material through appropriate citation. Plagiarism is a form of academic dishonesty, where ideas are presented falsely, either implicitly or explicitly, as being the original thought of the author's. The presentation of work, which contains the ideas, or work of others without appropriate attribution and citation, (other than information that can be generally accepted to be common knowledge which is generally known and does not require to be formally cited in a written piece of work) is an act of plagiarism. It can include the following:

- 1. Presenting work authored by a third party, including other students, friends, family, or work purchased through internet services;
- 2. Presenting work copied extensively with only minor textual changes from the internet, books, journals or any other source;
- 3. Improper paraphrasing, where a passage or idea is summarised without due acknowledgement of the original source;
- 4. Failing to include citation of all original sources;
- 5. Representing collaborative work as one's own;

Plagiarism is a serious academic offence. While plagiarism may be easy to commit unintentionally, it is defined by the act not the intention. All students are responsible for being familiar with the University's policy statement on plagiarism and are encouraged, if in doubt, to seek guidance from an academic member of staff. The University advocates a developmental approach to plagiarism and encourages students to adopt good academic practice by maintaining academic integrity in the presentation of all academic work.

| UCD Physics | Laboratory: Investigation of Springs |
|--|--------------------------------------|
| Student Name: Lab Partner Name: Lab Date/Time: | Student Number: Demonstrator Name |

What should I expect in this experiment?

You will investigate how springs stretch when different objects are attached to them and learn about graphing scientific data.

P(t)

0.004

Introduction: Plotting Scientific Data

In many scientific disciplines, and particularly in physics, you will often come across plots similar to those shown here.

Note some common features:

- Horizontal and vertical axes;
- Axes have labels and units;
- Axes have a scale;
- Points with a short horizontal and/or vertical line through them;





Why do we make such plots?

What features of the graphs do you think are important and why?

| | |
|------|------|
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |

The equation of a straight line is often written as y = m x + c.

y tells you how far up the point is, whilst x is how far along the x-axis the point is.

m is the slope (gradient) of the line, it tells you how steep the line is and is calculated by dividing the change in y by the change is x, for the same part of the line. A large value of m, indicates a steep line with a large change in y for a given change in x.

c is the intercept of the line and is the point where the line crosses the y-axis, at x = 0.



<u>Apparatus</u>

In this experiment you will use 2 different springs, a retort stand, a ruler, a mass hanger and a number of different masses.

Preparation

Set up the experiment as indicated in the photographs. Use one of the two springs (call this one spring 1). Determine the initial length of the spring, be careful to pick two reference points that define the length of the spring before you attach any mass or the mass hanger to the spring. Record the value of the length of the spring below.



Think about how precisely you can determine the length of the spring. Repeat the procedure for spring 2.

Calculate the initial length of spring 1.

Calculate the initial length of spring 2.

Procedure

Attach spring 1 again and then attach the mass hanger and 20g onto the spring. Measure the new length of the spring, using the same two reference points that you used to determine the initial spring length.

Length of springs with mass hanger attached (+ 20 g)

| | Spring 1 | Spring 2 |
|----------------------------------|----------|----------|
| Position of the top of spring | | |
| Position of the bottom of spring | | |
| New length of spring | | |

Add another 10 gram disk to the mass hanger, determine the new length of the spring. Complete the table below.

Measurements for spring 1

| Object Added | Total mass added to the spring (g) | New reference position (cm) | New spring length (cm) |
|--------------|--|--------------------------------|---------------------------|
| Disk 1 | 20 | | |
| Disk 2 | 30 | | |
| Disk 3 | | | |
| Disk 4 | | | |
| Disk 5 | | | |
| | | | |
| | | | |

Add more mass disks, one-by-one, to the mass hanger and record the new lengths in the table above. In the column labelled 'total mass added to the mass hanger', calculate the total mass added due to the disks.

Carry out the same procedure for spring 2 and complete the table below. Use the same number of weights as for spring 1.

Measurements for spring 2

| Object Added | Total mass added to the spring (g) | New reference position (cm) | New spring length (cm) |
|--------------|--|--------------------------------|---------------------------|
| Disk 1 | 20 | | |
| Disk 2 | | | |
| | | | |
| | | | |
| | | | |
| | | | |
| | | | |

Graphical Analysis

Add the data you have gathered for both springs to your graph on the following page. You should plot the length of the spring in centimetres on the vertical y-axis and the total mass added to the hanger in grams on the horizontal axis. Start the y-axis at -10 cm and have the x-axis run from -40 to 100 g. Choose a scale that is simple to read and expands the data so it is spread across the page. Label and give units your axes and include other features of the graph that you consider important.

Plot your graph by hand on this page and make your best estimate for a straight line fit to your data. *Note, your tutor will account for fitting done by hand.*



In everyday language we may use the word 'slope' to describe a property of a hill. For example, we may say that a hill has a steep or gentle slope. Generally, the slope tells you how much the value on the vertical axis changes for a given change on the x-axis. Algebraically a straight line can be described by y = mx + c where x and y refer to any data on the x and y axes respectively, m is the slope of the line (change in y/ change in x), and c is the intercept (where the line crosses the y-axis at x=0).

Suppose the data should be consistent with straight lines. Superimpose the two best straight lines, one for each spring, that you can draw on the data points. *Note, your tutor will account for your fitting by hand.*

Examine the graphs you have drawn and describe the 'steepness' of the slopes for spring 1 and spring 2.

Work out the slopes of the two lines.

What are the two intercepts?

How can you use the slopes of the two lines to compare the stiffness of the springs?

In this experiment the points at which the straight lines cross the y-axis where x = 0 g (intercepts) correspond to physical quantities that you have determined in the experiment. How well do the graphical and measured values compare with each other?

Look at the graphs on page 7, the horizontal and vertical lines through the data points represent the experimental uncertainty, or precision of measurement in many cases. In this experiment the uncertainty on the masses is insignificant, whilst those on the length measurements are related to how accurately the lengths of the springs can be determined.

How large a vertical line would you consider reasonable for your length measurements?

What factors might explain any disagreement between the graphically determined intercepts and the measurements of the corresponding physical quantity?

The behaviour of the springs in this experiment is said to be "linear". Looking at your graphs does this make sense?

| UCD Physics Laborate | ory: Investigating the Behaviour of Gases |
|--|---|
| Student Name: Lab Partner Name: Lab Date/Time: | Student Number: Demonstrator Name |

<u>Goal</u>

You will experimentally investigate the validity of a physical law. After this session, you will have more understanding of the process of experimental verification, and how the law you are testing is relevant to everyday experiences.

Specifically, you will test the Ideal Gas Law relating three variables of Volume, Pressure and Temperature using containers of air. To do this, you will keep one quantity fixed so that you can investigate how two other variables are related. In the first part you will keep the temperature constant and vary the volume to see how the pressure changes. In the second part you will keep the volume constant and vary the temperature to see how the pressure changes.

Warmup exercises

In this laboratory session, we investigate the relationship between the three properties of gases that we can most readily sense: volume, temperature and pressure. We call these macroscopic properties. But we understand that these properties derive from the movement of individual atoms/molecules (microscopic behaviour) that make up a gas, which move randomly, colliding with each other and the sides of the container.

- <u>Pressure, P</u>. The motion of billions of billions of gas particles in a container, causes them to collide with each other and with the sides of their container. In doing so they push on the sides of the container and we measure this as a pressure. For pressure, we use the S.I., unit of a force divided by an area, N/m² which is also called the Pascal, Pa.
- <u>Volume, V</u>. A gas is a collection of atoms and/or molecules that expands to fill any container of any shape. For volume, we use the S.I., unit of m³.
- <u>Temperature, T</u>. When a container of gas is heated, energy is transferred to the gas from a source of heat. Both the temperature and the internal energy (U) of the gas increase, and we find that T ∝ U. This internal energy is in the form of a kinetic (motion) energy for the molecules. The molecules move faster as the temperature of a gas increases. Likewise, when a gas is cooled, the molecules slow down.

Using the above information, circle the correct answers below:

| 0 | |
|---|---------------------|
| If you heat a gas, do the molecules move faster or slower? | faster / slower |
| If moving faster, do the molecules collide with the container walls | more / less |
| more, or less, frequently? | |
| If the molecules collide more frequently with the container walls, | increase / decrease |
| does the pressure increase or decrease? | |
| If you increase the container volume, are molecular collisions | more / less |
| more or less frequent? | |
| If the molecules collide less frequently, does the pressure | increase / decrease |
| increase or decrease? | |

Clearly, all three gas properties are interconnected, but how? If we keep one property fixed, we can investigate the relationship between the other two. For example:

- If we keep the gas temperature fixed, we can see how changes in volume affect pressure.
- If we keep the gas volume fixed, we can see how changes in temperature affect pressure.

These two relationships were first investigated by Irish scientist, Robert Boyle (1662), and French chemist, Gay-Lussac (1701). From the above information, can you figure out what remaining relationship was investigated by French scientist, J Charles (1780)?

A relationship between measurable quantities that is demonstrated experimentally and repeated in different ways over many years, can be said to be a physical law. Three scientists proved three relationships between the gas properties, leading to:

- Boyle's Law relating *P* and *V*.
- Gay-Lussac's Law relating P and T
- Charles' Law relating V and T

Since these three relationships are interconnected, we can combine them and we call the combined relationship *the Ideal Gas Law*, which is given by:

$$PV = nRT$$

where the constant of proportionality is the product of two constants, nR, where n is the number of moles of gas atoms/molecules there are and R is the ideal gas constant. Let's now test these ideas with two experiments.

Experiment 1: How the *pressure* of a gas changes when its *volume* is changed

Apparatus

- A pressure gauge, with a scale in units of pressure i.e. pascals (Pa).
- A sealed glass tube of gas (air), marked with



a scale of distance (mm) or volume (ml).

Procedure

- Open the tap (by turning it to a position parallel to the tube). Note the pressure reading. This is your baseline pressure; the pressure of the air all around us.
- Twist the adjustable screw to move the stopper to about a fifth of the way along the tube (as shown in the picture). This is simply a practical starting point for the number of readings to be conducted within the timeframe for the experiment.
- Close the tap to define a fixed amount/mass of gas. Record the baseline pressure.
- Twist the adjustable screw so that the stopper reduces the volume that the gas can occupy within the tube. As you do, notice what happens to the pressure reading. Take readings of pressure as you reduce the volume. (If the tube is marked with units of ml you can write down the volume directly in these units. If the tube is not in these units, you can calculate the volume of the gas by assuming the radius of the tube is 1 cm.)
- Estimate the accuracy of your measurements of volume and pressure.
- Open the tap, to release pressure, and unscrew the stopper to return it to its original position.
- Note: the equipment is only designed to work up to the maximum pressure on the scale. Keep below this pressure.

<u>Data</u>

| Volume (ml) | Pressure (Pa) | Estimate of error Volume measurements (m | in Estimated Error in Pressure nl) measurements (Pa) |
|----------------|------------------|--|--|
| | | | |
| | | | · · |
| | | | |
| | | | |
| | | | |
| | | | |
| | | | |
| | | | |
| | | | |
| | | | |
| | | | |
| | | | |

Do the following plots by hand on this page, or, use JagFit (see back of manual) and attach your two printed graphs to this page. Important: take care to label axes correctly and include units. *Note, your tutor will account for fitting where done by hand.*



Plot *P* along the y-axis, as a function of *V* along the x-axis:

Now plot *P* along the y-axis, as a function of 1/V along the x-axis:



From your graphs, describe how the gas properties are related. Is there a linear relationship between any two variables i.e., does a straight line fit to your points?

A straight-line graph is given by the equation y = m x + c, where m is the slope and c is the value of y where the line intercepts the y-axis i.e., where x = 0. Determine the slope and the intercept value, c, for your straight-line graph and give these values here, including units.

Do you expect the intercept to be at the origin where P = 0 and V = 0? Explain.

Conclusion

We investigated the relationship between pressure and volume, where temperature is held constant. This is Boyle's Law. From this experiment, briefly state this relationship in your own words and state if this is consistent with the Ideal Gas Law, for which $PV \propto T$.

Implications

When we inhale, we lower the diaphragm muscle to increase the volume of our lungs. When we exhale, we raise the diaphragm to decrease the volume. Relate this to differences in pressure between the inside and outside of the lungs with the aid of Boyle's Law (the Ideal Gas Law).



Explain another everyday example that relates pressure and volume (for a temperature that's approximately fixed), using the Ideal Gas Law.

Experiment 2: How the *pressure* of a gas change when its *temperature* is changed



<u>Apparatus</u>

• A sealed container of gas (air), connected to a heater.

• A white box containing connections to temperature and pressure sensors.

• Two multimeters, one to read pressure and one to read temperature.

Procedure

- Ensure all connections are in place (see picture).
- Turn the dial on the "pressure" multi-meter to V (volts), and press the "range" button until it is set to the millivolt (mV) range. You can record mV as a proxy for the units of pressure, Pascals (Pa). Set the "temperature" multi-meter to degrees Celsius (°C).
- Turn on the sensors, by checking that the white box is plugged in and then flipping the switch so that its light comes on. Record the temperature and pressure, as per the multi-meters.
- Turn on the heater, by checking that the large transformer is plugged in and then pressing the large green button so that the button lights up. At this point the gas is being heated and you will notice the temperature readings will slowly increase.
- Take temperature and pressure readings at intervals of about 5 °C until the temperature reaches about 80 °C. Then immediately switch off the heater by pressing the green button.
- Estimate the accuracy of your measurements of temperature and pressure.
- Turn off all equipment, by returning switches to original positions and disconnecting power.

<u>Data</u>

| Temperature (°C) | Pressure (Pa) |
|---------------------|------------------|
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |
| | |

| Estimated error in | Estimated Error in |
|--------------------|--------------------|
| Temperature | Pressure |
| measurements (°C) | measurements (Pa) |
| | |

<u>Results</u>

Plot pressure, P, (y-axis) as a function of temperature, T in °C (x-axis). Do this by hand on this page, or, use JagFit (see back of manual) and attach your printed graph to this page. Important: take care to label axes correctly and include units. *Note, your tutor will account for fitting where done by hand.*



From your graph, describe how the gas properties of pressure and temperature are related. Is there a linear relationship between any two variables i.e., does a straight line fit to your points?

The curve of a straight-line graph is given by the equation y = m x + c, where *m* is the slope and *c* is the value of *y* where the line intercepts the *y*-axis i.e., where x = 0. Determine the slope and the intercept value, *c*, for your straight-line graph and give these values here, including units.

From your values of *m* and *c*, *d*etermine the value of temperature in °C for which *P* would extrapolate to being zero.

Describe what the molecules of the gas would be doing in everyday language at this temperature, T_0 , for which P = 0?

Conclusion

We investigated the relationship between pressure and temperature, where volume is held constant. This is Gay-Lussac's Law. From this experiment, briefly state this relationship in your own words.

Explain how your measurements are consistent with the Ideal Gas Law, for which $PV \propto T$.

Implications

Car tyres increase in pressure by 3×10^4 N/m² after driving for 20 mins. Explain this with the aid of the Ideal Gas Law

A jam jar can be easier to open after warming it up in a bowl of hot water. Explain this with the aid of the Ideal Gas Law.

Explain another everyday example that relates pressure and temperature (for a volume that's approximately fixed), using the Ideal Gas Law.

| UCD Physics Labora | tory: Investigating Conservation of Momentum |
|--|--|
| Student Name: Lab Partner Name: Lab Date/Time: | Student Number: Demonstrator Name |

Goal

You will experimentally investigate the validity of a physical law. After this session, you will have more understanding of the process of experimental verification, and how the law you are testing is relevant to everyday experiences. You do not need prior knowledge of this topic to participate in this laboratory session.

Specifically, you will test the law of Conservation of Momentum, a law relating variables of mass and velocity, to explore the collision of two carts on a track. First, you will explore what happens when the carts have the same mass. Second you will explore what happens as you vary the mass of one of the carts.

Warmup exercises

We have an everyday understanding of the idea of momentum. It is a measure of how difficult it is to stop a moving object; the greater the momentum the harder it is to stop. We can appreciate that a truck moving at 30 km/s has more momentum than a small car moving at the same speed. Precisely, we define momentum, \vec{p} as:

$$\vec{p} = m\vec{v}$$

where *m* is the mass, and \vec{v} is the velocity. Momentum and velocity are vectors. A vector has a magnitude and a direction. For many objects, we can consider a combined (net) momentum and to do this we add up $m\vec{v}$ for each object.

In this laboratory, we consider motion in one direction only, and for this we are able to simplify the definition of momentum to the scalar relationship:

p = mv

where the values for p and v can be positive or negative to represent motion in the one direction or the other. We consider two colliding objects (carts) in our experiment. To find the combined (net) momentum for both carts, we simply add up the scalar value, mv for each cart.

A 10,000 kg truck is travelling eastwards at 100 km/s when it collides with a 1,000 kg parked car. Once they collide, the two vehicles travel together as a single unit. In which direction do they travel?

The car and truck move together after the collision. Do you expect their velocity to be greater, less or the same as the velocity of the truck before the collision? Why?

We find that the velocities of objects after a collision are not the same as beforehand, but we find that the combined (net) momentum after a collision, p_{after} is the same as that before the collision, p_{before} . This is called the law of <u>Conservation of Momentum</u>, and we can write this as:

$$p_{before} = p_{after}$$

Returning to the above question again, a 10,000 kg truck is travelling eastwards at 100 km/s when it collides head on with a 1,000 kg parked car. Once they collide, the two vehicles travel together as a single unit. In which direction do they travel and at what speed?

Hint: from considering Conservation of Momentum of motion in a straight line:

 $p_{before} = p_{after}$ $m_{truck}v_{before} = (m_{truck} + m_{car})v_{after}$

Solve:

| Ans: | | | |
|------|--|--|--|

To be termed a physical law, a relationship between measurable quantities must be demonstrated experimentally and repeated in different ways over many years. In this laboratory session, we will have a go at testing this law by causing a collision between two carts.

Before the collision, we will record the mass and the velocity of each cart, and add them together to find the net momentum before the collision. After the collision, we will again record the mass and velocity of each cart, and add them together to find the net momentum after the collision. We will test if the momentum before the collision is equal to the moment after. In this way, we will be experimentally testing the Law of Conservation of Momentum.

Experiment: Investigating Conservation of Momentum

Apparatus

• Two carts, of mass 0.5 kg each, which can travel along a low-friction track

• A wooden block, for hitting the cart release mechanism

• Two photogates connected to a blue data-logger, which reports the cart velocity at the gates

• Two metal bars, of mass 0.5 kg each, which can be added to the carts to increase their mass



Fig 1

PART A. Measuring the velocity of cart A before the collision

Experimental set-up

i) Setting up the cart on the track:

- Make sure the track is level, so that gravity does not affect the speed of the carts. This is done via an adjustable leg at one end.
- Note that one cart (let's call it cart A) has a spring-loaded bung which can be depressed to one of two positions. Depress the bung so that it is fully inserted into the cart and clicks into place there. (This can be tricky and seems to work best when holding the cart vertical.)
- Place cart A on the track at the opposite end to the pulley wheel, such that the bung can snap out and hit the end wall bumper when you hit the knob on top. Use the wooden block to hit the knob (it is more accurate than using your hand), and see how the cart travels along the track.
- Insert the rectangular metal "flag" into the hole at head of the cart, with the largest surface facing you. Make sure the flag is secure and does not move. (This can be achieved by lifting it slightly out of the hole.) The role of the flag is to interrupt the light beam of the photogates (see below).

ii) Setting up the two photogates:

In order to calculate momentum, we need values for mass and velocity. The cart mass is given as 0.5 kg. To calculate the velocity of the cart, we measure how long it takes the cart to travel a fixed distance between two points. The velocity is distance travelled divided by time taken. The distance between the two photogates is set using the ruler. The time taken is measured by the photogates.



Fig 2

- The photogates comprise an infrared light source on one side, and a detector on the other, fig 2. Infrared light is invisible to the human eye, but is represented by the red line in the figure. When the beam is interrupted it sends a signal to the blue data-logger to start the timer. When the cart interrupts the beam of the second photogate, that gate sends a signal to stop the timer.
- The data-logger uses this timer information, and pre-recorded distance, to compute the cart velocity which it outputs on the screen. To use this feature of the data-logger, it must be set up correctly.

iii) Setting up the blue data-logger:

- Check that the photogates work, by interrupting the light signal across the gate with your hand and checking that the red LED light on the gate blinks.
- Check that the data-logger reports a velocity each time the gate LED blinks. (Allow a slight delay in the data-logger response.)

Procedure

- Place the photogates at positions 40 cm and 80 cm on the track. In this way, the distance between the gates is 40 cm, which is the value we input during the data-logger set-up.
- On the data-logger, press 🕑 to begin recording data, and again after the cart has completed a run.
- Release cart A, and record its velocity. Repeat the measurement three times to get a good estimate. This is the velocity of cart A before the collision.

<u>Data</u>

Run five trials and fill in the following table.

Measurements on Cart A before the collision

The mass of cart A = _____ kg

| Trial number | Cart A velocity (m/s) | Cart A momentum <i>p</i> (kg m/s) |
|--------------|--------------------------|--------------------------------------|
| 1 | | |
| 2 | | |
| 3 | | |
| 4 | | |
| 5 | | |

Explain why you measure differing values for velocity (momentum) for each trial?

In the next part, cart A will be allowed to collide with a cart B which initially is stationary. In this case, the momentum of cart A before the collision constitutes the net (combined) momentum of both carts before the collision.

Using your above table of measurements, determine the following values for the net momentum before the carts collide:

| The average net | The minimum net | The maximum net | Uncertainty, given as: |
|-----------------------|----------------------------------|----------------------------------|--|
| momentum, <i>p</i> av | momentum, <i>p_{min}</i> | momentum, <i>p_{max}</i> | +/- (p _{max} – p _{min})/2 |
| (kg m/s) | (kg m/s) | (kg m/s) | (kg m/s) |
| | | | |

Note:

The difference in values, $p_{max} - p_{min}$, is called the spread of values. From this spread, we provide an estimate of uncertainty written as +/- $(p_{max} - p_{min})/2$. For example, this might be something like +/- 0.3. Uncertainty can in principle be analyzed in a more sophisticated way than this. However, a more precise analysis of a random variation requires at least ten measurements of that variable, and preferably more than thirty; something we won't do in this laboratory.

You have now measured the initial momentum and we will use these values later.

PART B. Measuring the velocity of cart A and cart B after the collision

Experimental set-up

i) Setting up the cart on the track:

• Place cart B on the track. Assume the head of the cart is the end with the velcro (which we will not be using in our experiment). Ensure its flag is securely in the hole at the head of the cart, with the largest surface facing you. Position cart B so that its rear points towards cart A.

ii) Setting up the photogates:

Move the first photogate to 50 cm and the second to 90 cm. We use a different technique to compute the velocity of the carts in this part of the experiment. In this part, the velocity is determined by how long it takes the metal flag to move past a given photogate. The data-logger measures how long the beam is interrupted for (i.e. time). It then uses the width of the flag (i.e. distance) to estimate the velocity of the cart. This is the reason we input the width of the flag (or flag length) when we first set up the data-logger. So the cart velocity is calculated from how long it takes its flag to pass through the photogate beam

iii) Setting up the blue data-logger:

Procedure

Release cart A, allowing it to collide with the rear end of cart B. Cart B will trigger the second photogate while cart A will trigger the first photogate. For this to occur, the rear of cart B should be initially positioned just under the first photogate (at 45 cm) so that its flag is positioned after the photogate.





<u>Data</u>

Run five trials and fill in the following table with your velocity measurements for the two carts after their collision. Also calculate the net momentum after the collision for each trial i.e., the combined momentum of both carts.

Case 1. After the collision, with cart A and cart B of the same mass

The mass of cart A = _____ kg The mass of cart B = ____ kg

| Trial number | Cart A velocity (m/s) | Cart B Velocity (m/s) | Net momentum after collision, <i>p</i> (kg m/s) |
|--------------|--------------------------|--------------------------|---|
| 1 | | | |
| 2 | | | |
| 3 | | | |
| 4 | | | |
| 5 | | | |

Determine the following three values from the above table:

| The average net | The minimum net | The maximum net | Uncertainty, given as: |
|---------------------------------|----------------------------------|----------------------------------|--|
| momentum, <i>p_{av}</i> | momentum, <i>p_{min}</i> | momentum, <i>p_{max}</i> | +/- (p _{max} – p _{min})/2 |
| (kg m/s) | (kg m/s) | (kg m/s) | (kg m/s) |
| | | | |

Now add a metal bar to cart B to increase its mass, and then repeat the five trials.

Case 2. After the collision, with 1 metal bar added to cart B

The mass of cart A = _____ kg The mass of cart B = ____ kg

| Trial number | Cart A velocity (m/s) | Cart B Velocity (m/s) | Net momentum after collision, <i>p</i> (kg m/s) |
|--------------|--------------------------|--------------------------|---|
| 1 | | | |
| 2 | | | |
| 3 | | | |
| 4 | | | |
| 5 | | | |

Determine the following three values from the above table:

| The average net | The minimum net | The maximum net | Uncertainty, given as: $\frac{1}{2}$ |
|-----------------|-----------------|-----------------|---|
| (kg m/s) | (kg m/s) | (kg m/s) | (kg m/s) |
| | | | |
| | | | |

Now add a second metal bar to cart B to increase its mass further, and then repeat the five trials again.

Case 3. After the collision, with 2 metal bars added to cart B

The mass of cart A = _____ kg The mass of cart B = _____ kg

| Trial number | Cart A velocity | Cart B Velocity | Net momentum after |
|--------------|-----------------|-----------------|------------------------------|
| | (m/s) | (m/s) | collision, <i>p</i> (kg m/s) |
| 1 | | | |
| 2 | | | |
| 3 | | | |
| 4 | | | |
| 5 | | | |

Determine the following from the above table:

| The average net | The minimum net | The maximum net | Uncertainty, given as: |
|-----------------------|----------------------------------|----------------------------------|--|
| momentum, <i>p</i> av | momentum, <i>p_{min}</i> | momentum, <i>p_{max}</i> | +/- (p _{max} – p _{min})/2 |
| (kg m/s) | (kg m/s) | (kg m/s) | (kg m/s) |
| | | | |
| | | | |

<u>Results</u>

Fill in the following tables.

Summary from part A:

| / I | | |
|------------------|---------------------------------|--|
| Before collision | Average net momentum, | Uncertainty, given as: |
| | <i>p_{av}</i> ,(kg m/s) | +/- (p _{max} – p _{min})/2 |
| | | (kg m/s) |
| | | |
| | | |

Summary from part B:

| After collision | Average net momentum, p _{av} (kg m/s) | Uncertainty, given as: +/- (p _{max} – p _{min})/2 (kg m/s) |
|---------------------------------|---|--|
| Carts of equal mass (case 1) | | |
| 1 bar added to cart B (case 2) | | |
| 2 bars added to cart B (case 3) | | |

From inspecting these tables, can you conclude that you have verified the Law of Conservation of Momentum? For this, consider if your measured net momentum before the collision matches that after the collision and consider the uncertainty in measurements.

As you increase the mass of cart B, does the total momentum after the collision change? Explain your answer.

Without altering your setup, how might you reduce the uncertainty in each value of average net momentum?

If plotting the velocity of cart B after the collision (y-axis) versus the mass of cart B (x-axis), what is the sign of the gradient for the graph? Zero, positive or negative?

Explain:

Conclusion

We sought to experimentally verify the Law of Conservation of Momentum, which for any two objects, *A* and *B*, can be written as:

$$p_{before} = p_{after}$$

 $m_A u_A + m_B u_B = m_A v_A + m_B v_B$

where *u* is the initial velocity, *v* is the final velocity, and *m* is the mass.

State the Law of Conservation of Momentum in your own words:

Implications

If your car was going to collide with an empty parked car, would you prefer the parked car to be heavier or lighter than your car? Why?

When a car crashes into a thick wall, we could say that it has momentum before the collision and that it is at rest after the collision. However, momentum must be conserved. Explain this apparent paradox by using the Law of Conservation of Momentum:

 $m_A u_A + m_B u_B = m_A v_A + m_B v_B$, and defining the variables for this case.

| UCD Physics Laboratory: Investigation of Electric Circuits | | |
|--|-----------------------------------|--|
| Student Name: Lab Partner Name: Lab Date/Time: | Student Number: Demonstrator Name | |

What should I expect in this experiment?

In this experiment you will carry out a number of investigations on simple electric circuits in order to determine some of their characteristics. Through these investigations you will develop rules of your electric circuit model which allow you to make predictions on other circuits.

Pre-lab assignment

Shown below are three arrangements of a bulb, battery one copper wire.



Choose the arrangements in which the bulb will light. You may choose more than one arrangement. Explain your answer.

Experiment 1: Current

In this and the second electronics experiments, you will develop a model for electric circuits. The development of your model will always be guided by the observations you make. All reasoning you do to make predictions should be based on your model only, not on prior knowledge of electric circuits.

In this experiment you begin your investigation of electric circuits and some of their properties. Starting from the basics of electric circuits, you will develop a consistent model of simple resistive circuits.

Make sure you check your answers with a demonstrator when asked to do so.

Equipment/Apparatus check

Check that you have at your disposal: a battery, a 2.5V bulb and a single wire.

Section 1: Complete Circuits

i. Consider the three arrangements of a battery, a bulb and a single wire in the pre-lab assignment. Use your pre-lab answers to complete the "Idea" column of the table below.

| Arrangement | Idea (on/off) | Observation (on/off) |
|-------------|---------------|----------------------|
| 1 | | |
| 2 | | |
| 3 | | |

ii. Connect the circuits and verify your ideas, enter your observations in the final column of the table.

WARNING: Some arrangements may cause the wire to get hot.

iii. There are three other arrangements of the battery, bulb and wire in which the bulb lights. Find the other arrangements in which the bulb lights and sketch these in the space below.

An arrangement of a battery, bulb, and wire in which the bulb lights is said to be a **closed electric circuit**. Such an arrangement can also be referred to as a **complete circuit**, or just a **circuit**.

iv. Explain in your own words why this is a sensible name. Refer to the arrangements in which the bulb lit, and to those in which the bulb did not light.

v. What do you think is meant by an open circuit?

vi. Formulate a **rule** which defines the nature of a circuit


Section 2: Conductors and Insulators

In the previous section you arranged a battery, bulb and wire in such a way that the bulb lights. In this section we will investigate the effects that different materials have on an electric circuit.

Equipment/Apparatus check

Retain the equipment from Section 1, you will also need a battery holder, three bulb holders, four extra wires, two extra 2.5V bulbs. Take a selection of sample materials from those provided in the lab.

i. Use the battery, battery holder, bulb, bulb holder and two wires to set up the circuit shown in Figure 2.1a below. This we will call a single bulb circuit.



Figure 2.1: (a) Single bulb circuit and (b) corresponding circuit diagram.

ii. Insert each of your sample objects (e.g. paper, elastic band, crocodile clip and bulb clip) individually into the circuit as shown in the diagram at right and write down any effects you note on the brightness of the bulb. Consider clearly visible differences only.



Figure 2.2: Circuit with bulb and elastic band.

iii. The objects that allow the bulb to glow are called **conductors**. Objects that cause the bulb to go out are called **insulators**. Categorise the materials according to how they affect the brightness of the bulb. Make a table with an appropriate caption in the space below, and enter your results.

iv. Using circuits like that of Figure 2.3 below, determine whether each part of the bulb shown in Figure 2.4 is a conductor or an insulator.



Figure 2.3: Investigating the properties of a bulb.



| Material | Property |
|--------------|----------|
| Glass | |
| Metal casing | |
| Black disk | |
| Metal tip | |

Based on your investigations thus far, which of the following diagrams do you think best represents the connections of the filament inside a bulb? Explain.



Figure 2.5: Possible filament arrangement inside a bulb.

Considering your results from the previous two questions, what do you feel is the purpose of the black disc at the base of the bulb?

Discuss your answers to sections 1 and 2 with a demonstrator.

Section 3: Current

While you carry out the following experiments it is helpful to make the following two assumptions.

- 1. There is a flow around a circuit; we will call this flow current.
- 2. Bulb brightness indicates the amount of current. An increase in brightness indicates an increase in current.

These assumptions form the base of our **model** for electric circuits. As we continue our experiments, we will check whether the model holds, and expand it to gain a deeper understanding of electric circuits.

Take the above information into consideration when answering the following questions:

i. Explain how the first assumption, that there is a flow (current) around a circuit, is consistent with the idea that a complete circuit is needed for a bulb to light.

Can you tell the direction of current from your observations? Explain.

ii. If you were to connect a wire across the terminals of a battery, you would notice that the wire and battery get hotter in such a way that points 1, 2, and 3 are always equally hot, and the hotter they get the hotter the battery gets.



Figure 3.1 Hypothetical set-up of a battery and a wire.

Do not carry out this experiment

From this observation and building on your model for electric circuits, what can we assume about the flow of the current.

iii. Base your answers to the next two questions on the assumptions given at the start of this section. If two identical bulbs are equally bright, what does this indicate about the current through them?

If one bulb is brighter than another identical bulb, what does this indicate about the current through the brighter bulb?

Check your answers with your demonstrator before proceeding

Section 4: Series Circuits

i. Before you construct the circuit shown in Figure 4.1a, predict how the brightness of bulb B will compare to that of bulb C. Make the prediction first.

When asked to make predictions about a circuit, you should be able to determine your answer from your model. Do not deprive yourself of an opportunity to check on your progress by skipping the prediction and carrying out the experiment straight away. (a) (b) B Figure 4.1: (a) A two-bulb series circuit and (b) corresponding circuit diagram. How do you think the brightness of bulbs B and C will compare to that of a single bulb circuit? Explain. ii. Construct the circuit shown above and compare your predictions with your observations. This circuit is called a series circuit.

iii. Based on your model, how does the current through battery 1 in figure 4.2 compare to that through bulb A?



Figure 4.2 Single-bulb and two-bulb series circuits.

How does the brightness of bulb A compare to the brightness of bulb B, and what can you can conclude about the current through bulb A in comparison to the current through bulb B?

Based on your previous two answers, how does the current through bulb B compare to the current through battery 1?

How does the current through bulb B compare to the current through bulb C?

How does the current through bulb B compare to the current through battery 2? Make sure you use your model to answer this question.

Finally, considering your answers to the previous questions, how does the current through battery 1 compare to the current through battery 2?

iv. Summarise your answers to part iii by ranking the currents i1, i2, iA, iB, and iC in Figure 4.3 from greatest to least. If any currents are equal, state so explicitly.

i1 : Current through battery 1i2 : Current through battery 2iA : Current through bulb AiB : Current through bulb B

iC : Current through bulb C

Figure 4.3: Single-bulb and two-bulb series circuits.

Explain your reasoning.

If a third bulb were placed in series with bulbs B and C, do you think it would light? Do you think the current through bulbs B and C would increase, decrease, or remain the same? Set up the circuit and test your predictions.

Check your answers with a demonstrator before proceeding

Section 5: Current Measurement

In this section, we introduce an instrument called an ammeter that allows us to measure current. An ammeter must be connected in series in the circuit. The ammeter used in this experiment measures the current through the circuit in milliampere (mA), which is 1/ 1000 of an ampere.

$$--A^+$$

Figure 5.1: Ammeter circuit symbol.

Notice that one terminal of the ammeter is marked positive and the other negative. If you follow a continuous path from the positive terminal of the ammeter to the battery, you should get to the positive terminal of the battery first. We will say that the positive terminal of the ammeter is **electrically closest** to the positive terminal of the battery.

WARNING: If you are not sure which way to connect the ammeter leads, connect just one lead, then tap the second lead in place to make a fleeting contact while you are watching the meter. If the needle jumps the wrong way, reverse the leads.

i. Connect an ammeter in series with a bulb in a single bulb circuit as shown in Figure 5.2 where the positive terminal of the battery (the battery nub) is connected to the red terminal of the ammeter. Connect the black terminal of the ammeter to the bulb. Write down the ammeter reading:

Compare the circuit diagram to the circuit layout. How can you tell from the circuit diagram which battery terminal is positive?



Figure 5.2: (a) Ammeter in a single bulb circuit and (b) corresponding circuit diagram.

ii. Predict what would happen to the reading on the ammeter if you were to add a second bulb in series with bulb A.

iii. Set up the series circuit shown in Figure 5.3, and note the reading on the ammeter. Compare your prediction to your observation. Is the reading on the ammeter consistent with your observations in the previous section?





Figure 5.3: Circuit diagram for a two-bulb series circuit with ammeter.

Now place the ammeter in between bulbs B and C as shown in Figure 5.4. How does the reading compare to the previous reading?



How does the current that enters bulb B compare to the current that leaves bulb B?

What do you think the current will be when it leaves bulb C?

Test your prediction.

Figure 5.5: Ammeter after two bulbs in series.

iv. A student measures that the current through battery 1 is equal to 100 mA, and the current through bulb B is equal to 70 mA. The batteries are identical; so are the bulbs. What values would this student measure for the current through bulb A, battery 2 and bulb C? Explain.



Check your answers with a demonstrator before proceeding

Section 6: Electrical Resistance and Voltage

In the Current excercise we discovered some properties of basic electric circuits. These laid the foundations for our model of electric circuits. We will treat the two assumptions we made:

1. that there is a flow called current in a complete circuit, and that

2. the brightness of a bulb indicates the magnitude of the current through it, as the first two rules of our model. In this experiment we expand our model and broaden

our understanding of electric circuits by investigating other types of circuits.

Equipment/Apparatus Check

Check to make sure you have a power supply, an ammeter, six wires, three bulb holders, three 6.5V bulbs and two crocodile clips.

Section 7: Power Supply

In the Current experiment you worked solely with batteries, bulbs and wires. In this experiment you will use a new component called a power supply.



Figure 7.1 A single bulb connected to a power supply



Figure 7.2 Two bulbs in series connected to a power supply

.

WARNING: The two leads of the power supply should not touch each other directly or be connected through a wire only.

i. Attach two crocodile clips to the leads of the power supply and set up a single bulb circuit as shown in the diagram at right. The switch on the power supply should be set to 9 V.

ii. Now added a second bulb and verify that the behaviour is as expected.

Section 8: Resistance in Series Circuits

In what follows, you may assume that a power supply and a battery behave identically. In the last electronics experiment we observed that when a bulb was added in series, the bulbs in the circuit dimmed. We took this as evidence that the current through the bulbs and the battery decreased. We now try to incorporate this finding into our model for electric circuits.



Figure 8.1 Adding a third bulb in series.

i. Consider the two bulb series circuit that you set up in Section 7. We label the bulbs A and B. Predict what would happen to the brightness of bulb A if a third bulb were added in series to the circuit as shown in the figure above.

ii. Set up the circuit and verify your prediction.

To explain why the brightness of bulbs and the magnitude of current through the battery is different in different circuits, it is helpful to think of bulbs as providing an obstacle or a **resistance** to the flow of current. In this picture, an increase in the circuit's resistance causes a decrease in current through the battery and vice versa.

iii. What can you infer about the total resistance of a circuit as more bulbs are added in series?

iv. Formulate a **rule** which allows you to predict how the current through the battery would be affected as the number of bulbs added in series were increased or decreased. Include the concept of resistance in your rule. **This is the third rule of our model**, to go with the two rules you made in the first electronics experiment.



Section 9: Parallel Circuits

We have seen how adding bulbs in series affects the current through the battery and how it affects the brightness of the bulbs in the circuit. We now look at a different circuit and compare its properties to that of the circuits we have seen previously. The circuit shown in Figure 9.1 is called a **parallel circuit**.



Figure 9.1 Two bulbs in parallel.



Figure 9.2 Single bulb circuit.

i. Compare the circuit diagram of the parallel circuit above to that of a single bulb circuit shown in Figure 9.2 to the right.

What are the similarities and differences between the two circuits represented by the diagrams? How many complete conducting routes/pathways exist in each circuit?

In a parallel circuit we often think of the current splitting and node recombining at junctions or nodes in the circuit. A junction or node can be defined as an electrical connection between three or more components. Figure 9.3 A node. Draw nodes on figure 9.4, where appropriate.

Figure 9.4 Circuit diagram without nodes.

ii. Predict how the brightness of each bulb in a parallel circuit will compare to that of a bulb in a single bulb circuit?

Set up the parallel circuit from Figure 9.1 using bulbs and a 9V power supply. Write down your observations below.

Compare the brightness of each of the bulbs in parallel. How do the currents through the bulbs compare to each other?

Section 10: Resistance in parallel circuits

We have seen that when we add a bulb in series to a single bulb circuit the current through the battery decreases. We now carry out more experiments to investigate the properties of parallel circuits.

Figure 10.1 A two bulb series circuit



i. Set up a two bulb series circuit as in Figure 10.2. We call bulb A an **indicator bulb** as, throughout this experiment, it indicates the current through the battery.

Suppose that you added a third bulb, C, in parallel with bulb B as shown in figure 10.2.



Figure 10.2 A three bulb circuit

Do you expect the brightness of bulb A to change when bulb C is added? Explain briefly

Predict how the brightness of the bulbs in the diagram of Figure 10.2 would rank from greatest to least. Carefully explain how you used your model to make your prediction.

ii. Now add bulb C in parallel to bulb B as shown in figure 10.2. How does the brightness of the indicator bulb A change?

iii. What can you infer about the change in the resistance of the circuit as bulb C is added in parallel to bulb B?

Is your answer consistent with what you found in Section 9 when you added a bulb in parallel with a single bulb? Explain briefly.

Check your rule with your demonstrator

Section 11: Measurement of current

In this section, we make a series of measurements that will add some quantitative evidence to the observations made in the previous section.

i. Use an ammeter to measure the current in a single bulb circuit as shown in Figure 11.1. Write down your measurement below.



ii. In the circuit of Figure 11.2, the ammeter is measuring the current through one of the bulbs in a parallel circuit. On the basis of your observations and measurements, predict the reading on the ammeter.



Figure 11.2 Parallel circuit with ammeter in one of the branches

Set up the circuit and verify your prediction.

iii. Based on your observations from the previous section, **predict** the reading on the ammeter when it is connected to read the current through the battery in a parallel circuit as shown in Figure 11.3 below.

Explain briefly



Figure 11.3 Parallel circuit with ammeter reading current through the battery.

Set up the circuit as shown in Figure 11.4, and verify your prediction.

iv. Compare the current through the battery in the parallel circuit to the current through the battery in the single bulb circuit. Do your measurements support the idea that the current through a battery can be different in different circuits?



Figure 5.4 Parallel circuit with ammeter reading Current through the battery.

What can you infer about the resistance of a parallel circuit as compared to that of a single bulb circuit?

vi. Revise the third rule that you formulated in Section 8, so that it describes how the current through the battery changes when a bulb is added in parallel or in series to a circuit. Include the concept of resistance in your rule. Make sure you rule incorporates the results from Sections 9,10 and 11.

Discuss your answers with your demonstrator

| UCD Physics Laboratory: Investigation of Acceleration | | | | |
|---|--------------------------------------|--|--|--|
| Student Name: Lab Partner Name: Lab Date/Time: | Student Number: Demonstrator Name | | | |

Goal

You will experimentally investigate the validity of a physical law. After this session, you will have more understanding of the process of experimental verification, and how the law you are testing is relevant to everyday experiences. You do not need prior knowledge of this topic to participate in this laboratory session.

Specifically, you will test Newton's 2nd Law, a law relating three variables of force, mass and acceleration, using a cart on a track. To do this, you will keep one quantity fixed so that you can investigate how two other variables are related. In the first part you will keep the force in the direction of motion (along the horizontal) fixed and relate a horizontal acceleration to a mass. In the second part, you will keep the mass fixed and relate the acceleration down a slope to the component of the gravitational force directed down the slope.

Warmup exercises

Newton's second law is given by the vector relationship, $\overline{F} = m\overline{a}$, for which a force causes an acceleration and the constant of proportionality is mass, *m*. However, for motion confined to a straight line (one dimensional motion), we can simplify this law to the scalar relationship, F = m a, where *F* is the value of the net force acting on an object along its allowed direction of motion, and *a* is the value of acceleration in this direction of motion. We consider only motion in a straight line in this laboratory and so we are able to use this scalar form of the law.

If you throw a heavy ball with a force F and then throw a light ball with the same force, which ball gathers more speed?

Acting under constant acceleration, a cart starts from rest and has a horizontal velocity of 2 m/s due west after 5 s. What is the acceleration of the cart?

Forces cause acceleration. For example if you kick a ball of mass m with a force 'F', its acceleration is 'a'; if you then kick the same ball with a force twice as big, '2F', then it accelerates at '2a'. In other words, the acceleration, a, is larger when the force, F, is larger:

 $a \propto F$

The acceleration is larger when the mass, m, of the object is smaller:

$$a \propto \frac{1}{m}$$

We can combine these two relationships into one:

$$a \propto \frac{F}{m}$$

Isaac Newton (1687) provided experimental evidence of this relationship, and so it became a 'Law'. It is now called <u>Newton's 2nd Law</u>, and is more commonly written as:

$$F = m a$$

The unit of force is kg·m/s² which is called the Newton (symbol N), in honour of Isaac Newton.

If an apple falls from a tree, it speeds up until it hits the ground. So there must be a force which causes this acceleration. The acceleration due to the Earth's gravitational force field has been measured experimentally to be 9.8 m/s². We denote this as 'g' since its value is always the same, instead of generic acceleration 'a' (which can have many values). So the gravitational force is the product, mg.

To test Newton's 2nd Law, you will keep one quantity fixed so that you can investigate how two other variables are related. In the first part you will keep the force fixed and relate a horizontal acceleration to a mass which is varied. In the second part, you will keep the mass fixed and relate the acceleration to a force which is varied.

<u>Apparatus</u>

- One cart, of mass 0.5 kg
- A low-friction track, with a pulley wheel on one end
- A string, with a disk tied to one end and a hook to the other, threaded over the pulley wheel
- Two photogates connected to a blue data-logger

• Three metal bars, of mass 0.5 kg each, which can be added to the cart to increase its mass

Where using a pulley, the string has an equal tension throughout. This simplifies our thinking, because we can consider the stage as being accelerated horizontally due to a constant horizontal force of magnitude, F, and we also consider F to be the magnitude of force exerted vertically between the string and the hook-mass. We return to this with an equation later.

Experiment 1: Acceleration from a constant force along a horizontal plane

Experimental set-up



Fig 1

i) Setting up the cart on the track:

- Position the track on the laboratory bench in such a way that the pulley wheel hangs over one end of the bench.
- Ensure the track is level. This is done via an adjustable leg at one end.
- Place the cart on the track at the opposite end to the pulley wheel.
- You will find a string, with a disk tied to one end and a hook to the other. Attach the string to the cart (by simply placing the disk on the cart), and thread the string over the pulley wheel so that the hook hangs down.
- Attach a 10 g mass to the hook, and see how this causes the cart to accelerate along the track.
- Insert the rectangular metal "flag" into the hole at head of the cart, with the largest surface facing you. Make sure the flag is secure and does not move. (This can be achieved by lifting it slightly out of the hole.) The role of the flag is to interrupt the light beam of the photogates (see below).

ii) Setting up the two photogates:

- The photogates comprise an infrared light source on one side, and a detector on the other, fig 2. Infrared light is invisible to the human eye, but is represented by the red line in the figure. When the beam is interrupted it sends a signal to the blue data-logger.
- Place the photogates at positions 30 cm and 80 cm on the track. In this way, the distance between the gates is 50 cm.
- In order to calculate acceleration, we must measure the change in velocity in a given time interval.
- The velocity is determined by how long the cart's metal flag takes to move past a given photogate. The photogate is connected to a blue data-logger, which reports how long the beam is interrupted for (i.e. time). It then uses the width of the flag (i.e. distance) to estimate the velocity of the cart. For this reason, we must input the width of the flag (or flag length) when we set up the data-logger (below). The cart *velocity* is calculated from how long it takes its flag to pass through the photogate beam. To output these results, the blue data-logger must be set up correctly (see below).

• The cart *acceleration* is determined by computing the change in velocity between the two photogates.



Fig 2

iii) Setting up the blue data-logger:

- Turn on the power supply at the socket. Turn on the blue data-logger. A screen will appear, select "photogate timing" and enter the flag length (0.0250 m) and photogate spacing (0.5000 m) by pressing 🕑 to edit and again to confirm.
- Ensure that only 'Velocity In Gate' and 'Time Between Gates' are set to visible.
- Then press the home key.
- Press F1 or navigate to the graph section. Once on the graph screen, press F4 to open the graph menu. Navigate to 'Two Measurements' and press select.
- Press the select key and navigate to the 'Y' (i.e. y-axis), which should be visible on the right-hand side of the graph. Press select and choose 'Time Between Gates'. This will now appear on the right of the graph. The left axis should already be displaying "Velocity in Gates".
- You can now record data by pressing O to begin and stop.
- On the graph screen, velocity will be displayed as a line and the time taken to travel between gates will be displayed as both a single point on the graph and as a numerical value along the right-hand side Y axis of the graph.
- To read the data from your completed run accurately, press F3 and select 'Smart Tool'. Use the navigation buttons to see the precise values for the points on the graph.
- To save your experimental data, use the arrow keys to highlight your data file in the RAM memory and press "F4 files". Select the "copy file" option and then choose the external USB as the destination for the file, and press "F1 OK". Transfer the USB data stick to the lab computer, and create a graph.

Procedure

- On the data-logger, press 🕑 to begin recording data, and again after the cart has completed a run.
- Record the total mass being accelerated (i.e. the mass of the cart, the metal block on the cart, the hook, the additional mass on the hook). Release the cart, and record its velocity and time as it passes each photogate.
- Add a metal bar to the cart to increase its mass, and repeat the above steps.
- Repeat until you have added three metal bars. Be sure that the metal bars are not stacked too high i.e. that they do not trigger the photogate.

Data:

| Mass of | Mass of | Velocity | Velocity | Time 1, | Time 2, | Acceleration, |
|-------------------------------|-------------------------------|----------------------------------|--------------------------|---------|---------|---------------|
| hook, <i>m_{hook}</i> | cart, <i>m_{cart}</i> | 1 , <i>v</i> ₁ | 2, <i>v</i> ₂ | t_1 | t_2 | а |
| (kg) | (kg) | (m/s) | (m/s) | (s) | (s) | (m/s²) |
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |

• Calculate the acceleration (i.e. the change in velocity during a given time interval):

$$a = \frac{v_2 - v_1}{t_2 - t_1}$$

• On the blue data-logger, use the arrow keys to highlight your data file in the RAM memory and press "F4 files". Select the "copy file" option and then choose the external USB as the destination for the file, and press "F1 OK". Before transferring the USB data stick to the lab computer to create a graph, we must decide what to put on the x and y axes (see below).

Results

If Newton's 2nd Law is indeed, F = m a, it will plot as a straight line i.e., it will take the form:

$$y = kx + c$$

where k is the gradient (slope), and c is what we will call the intercept (the value of y where x is zero). Here we refer to k instead of the traditional m for the gradient of a straight line, because we have already used m to mean mass.

In this investigation, we kept the force constant and increased the mass in order to investigate how acceleration changes. Therefore, we put mass on the x-axis and acceleration on the y-axis. How can we rearrange Newton's 2nd Law into the mathematical format of a straight line graph, where the x-axis is the mass and the y-axis is the acceleration?

We could rearrange F = m a into the format y = k x + c as follows:

$$\frac{1}{a} = \frac{1}{F} m$$

where *a* is acceleration, *F* is force, *m* is mass and c = 0

| i) $m - m$ | |
|--------------------------------|--|
| 1 $11 - 11$ cart | |
| ii) $m = m_{hook}$ | |
| iii) $m = m_{cart} + m_{hook}$ | |
| iv) $m = m_{cart} - m_{hook}$ | |

The cart and hook are connected together and so they have the same magnitude of acceleration, *a*, and the net mass moving is $m_{cart} + m_{hook}$. Thus, we can more usefully rearrange our equation as follows:

$$\frac{1}{a} = \frac{1}{F} (m_{cart} + m_{hook})$$
$$= \frac{1}{F} m_{cart} + \frac{1}{F} m_{hook}$$

Now, for this case where $\frac{1}{a}$ is the y-axis and m_{cart} is the x-axis, which term is the slope of this graph? And which term is the intercept i.e., the value of *y* where *x* is zero?

Plot your experimental data, with $\frac{1}{a}$ as the y-axis and m_{cart} as the x-axis. If the graph is a straight line, then you have verified Newton's 2nd Law.

Plot your graph by hand on this page and make your best estimate for a straight line fit to your data. *Note, your tutor will account for your fitting by hand* Important: take care to label axes correctly and include units.



You can now find a value for *F* in two separate ways and compare them for accuracy, as follows:

From your graph determine the slope, and hence calculate *F*.

From your graph determine the intercept, and hence calculate *F*.

Compare your value of F determined in the two different ways above, determine the best value of F and estimate the uncertainty on your resulting value for *F*.

From the value you found for F, calculate the acceleration due to gravity, g. How does it compare to the generally accepted value of g?

Hint: because we use a pulley, the force, *F* also acts vertically on the hook. The vertical motion of the hook can therefore be considered under solely this tension force *F* and the force due to gravity, $m_{hook}g$.

Experiment 2: Acceleration of a constant mass down an inclined plane



The apparatus should be set up as in the picture. Raise one end of the track using the wooden block in place of the elevator. The carts can be released from rest at the top of the track.



The cart will experience a gravitational force, given by $F_g = m \cdot g$ directed vertically downwards towards the earth, where the acceleration due to gravity is g directed vertically downwards (see diagram). By taking components of a vector, it is possible to show that the component of the gravitational force directed along our permitted direction of motion down the slope, is $F_{g} \cdot sin\theta$, which is then equal to $mg \cdot sin\theta$. This force causes the cart to accelerate and roll down the slope. From our warmup exercises in this script, we were saying that for Newton's second law, F = m a, where F is the value of the net force acting on an object along its allowed direction of motion, and a is the value of acceleration in the object's direction of motion. And so, from Newton's Second Law, we can write:

$$F_{g} \cdot \sin\theta = mg \cdot \sin\theta = ma$$

where *a* is the component of the object's acceleration parallel to the inclined plane.

By cancelling *m*, this simplifies to: $a = g \cdot sin\theta$ (as shown in the diagram)

In keeping with intuition then, the acceleration of the cart depends on the angle of the incline. For example, a = 0 where $\theta = 0$, and a = g where $\theta = 90^{\circ}$.

Procedure

Vary the angle of the incline, taking measurements using the data-logger for at least four different angles, and determine the accelerations for the cart in the same way as was done in investigation 1.

Data:

| Angle incline | of | Sine of angle | <i>v₁</i> (m/s) | <i>v</i> ₂ (m/s) | <i>t</i> ₁ (s) | <i>t</i> ₂ (s) | Acceleration down the incline, <i>a</i> (ms ⁻²) |
|------------------|----|---------------|-----------------|-----------------------------|---------------------------|---------------------------|---|
| | | | | | | | |
| | | | | | | | |
| | | | | | | | |
| | | | | | | | |
| | | | | | | | |
| | | | | | | | |

Since we predict that the acceleration down the incline is $a = g \sin \theta$, we expect there to be a linear dependence of *a* on $\sin \theta$.

Make a graph with $\sin\theta$ as the *x*-axis and *a* as the *y* axis to see if this is the case.

What does the slope represent?

What value do you expect (theoretically) for the intercept?

Plot your graph by hand on this page and make your best estimate for a straight line fit to your data. *Note, your tutor will account for your fitting by hand.* Important: take care to label axes correctly and include units.



What value do you measure for *g*?

What value do you measure for the intercept?

Comment on your results. How could you improve on your measurements of g?

Conclusion

We sought to experimentally verify Newton's 2nd Law, F = m a. State Newton's 2nd Law in your own words:

Implications

If you simultaneously drop a bowling ball and a billiard ball, they will hit the ground at the same time. This means that they were both accelerated at the same rate. What is this rate?

Does the bowling ball experience a larger, smaller or the same force as the billiard ball? Use Newton's 2nd Law to justify your answer.

The single scalar form for Newton's second law is helpful to consider for straight line motion. For more general motion in three dimensions, for example along *x*, *y* and *z* axes, the vector form of Newton's Second Law yields three scalar relationships: $F_x = m a_x$, $F_y = m a_y$ and $F_z = m a_z$. In this way, we are able consider motion in each orthogonal direction as being independent.

Give a common example for which in principle we need to consider the vector form of Newton's second law. *Hint: can you think of a common motion that is generally isn't in a straight line?*

| UCD Physics Laboratory: | Investigation of Electrical Circuits 2 |
|--|--|
| Student Name: Lab Partner Name: Lab Date/Time: | _ Student Number: _ Demonstrator Name |

What should I expect in this experiment?

In this experiment you will carry out more investigations on simple electric circuits in order to determine some more of their characteristics. Through these investigations you will develop more rules of your electric circuit model which allow you to make predictions for other circuits.

Pre-lab assignment

In your own words describe what is meant by electrical current and electrical resistance. In the circuit below all the bulbs are identical.

How does the brightness of bulb A compare to the brightness of bulb B?

Choose one answer.

- o Bulb A is brighter than bulb B
- o Bulb A is as bright as bulb B
- o Bulb A is dimmer than bulb B
- o I do n't know



Explain your answer to the previous question. How does the brightness of bulb A compare to the brightness of bulb C?

Introduction

In the Current laboratory we discovered some properties of basic electric circuits. These laid the foundations for our model of electric circuits. We will treat the two assumptions we made: that there is a flow called current in a complete circuit, and that the brightness of a bulb indicates the magnitude of the current through it, as the first two rules of our model. In today's experiment we expand our model and broaden our understanding of electric circuits by investigating other types of circuits.

Equipment/Apparatus Check

Check to make sure you have a power supply, an ammeter, six wires, three bulb holders, three bulbs and two crocodile clips.

Section 1: Power Supply

In the Current laboratory you worked solely with batteries, bulbs and wires. In this experiment you will use a new component called a power supply.

i. Attach two crocodile clips to the leads of the power supply and set up a single bulb circuit as shown in the diagram at right. The switch on the power supply should be set to 9 V.



Figure 1.1 A single bulb connected to a power supply

WARNING: The two leads of the power supply should not touch each other directly or be connected through a wire only.

ii. Do you think the brightness of the bulb would change if another bulb were added in series to the circuit as shown in Figure 1.2? Explain.

Set up the circuit shown at right and verify your ideas. What did you observe?.



Figure 1.2 Two bulbs in series connected to a power supply

iii. How do your observations compare to your observations from the Current laboratory? Do the circuits containing a battery behave differently to circuits containing a power supply or do they behave the same?

Section 2: Resistance in Series Circuits

In what follows, you may assume that a power supply and a battery behave identically. In the last electronics experiment we observed that when a bulb was added in series, the bulbs in the circuit dimmed. We took this as evidence that the current through the bulbs and the battery decreased. We now try to incorporate this finding into our model for electric circuits.



Figure 2.1: Adding a third bulb in series.

i. Consider the two bulb series circuit which you have set up in Section 1. We label the bulbs A and B. Predict what would happen to the brightness of bulb A if a third bulb were added in series to the circuit as shown in Figure 2.1 above.

ii. Set up the circuit and verify your prediction.

To explain why the brightness of bulbs and the magnitude of current through the battery is different in different circuits, it is helpful to think of bulbs as providing an obstacle or a **resistance** to the current. In this picture, an increase in the circuit's resistance causes a decrease in current through the battery and vice versa.

iii. What can you infer about the total resistance of a circuit as more bulbs are added in series?

iv. Formulate a rule which allows you to predict how the current through the battery would be affected as the number of bulbs added in series were increased or decreased. Include the concept of resistance in your rule. This is the third rule of our model, to go with the two rules you made in the first electronics laboratory.

Discuss your answers with your demonstrator.

Section 3: Parallel Circuits

We have seen how adding bulbs in series affects the current through the battery and how it affects the brightness of the bulbs in the circuit. We now look at a different circuit and compare its properties to that of the circuits we have seen previously. The circuit shown in Figure 3.1 is called a **parallel circuit**.





Figure 3.1: Two bulbs in parallel.

Figure 3.2: Single bulb circuit.

i. Compare the circuit diagram of the parallel circuit above to that of a single bulb circuit shown in Figure 3.2 to the right. What are the similarities and differences between the two circuits represented by the diagrams? How many complete conducting routes/pathways exist in each circuit?

ii. How do you think the brightness of each bulb in a parallel circuit will compare to that of a bulb in a single bulb circuit?

Set up the parallel circuit as shown below in Figure 3.3. Compare the brightness of the bulbs in the parallel circuit to that of a bulb in a single bulb circuit. Write down your observations below.

Figure 3.3 Parallel circuit set-up

Compare the brightness of each of the bulbs in parallel. How do the currents through the bulbs compare to each other?

In a parallel circuit we often think of the current splitting and recombining at junctions or nodes in the circuit. A junction or node can be defined as an

Figure 3.4 A node

electrical connection between three or more components.



Figure 3.4: A node.

Draw nodes on figure 3.5, where appropriate.



Figure 3.5: Circuit diagram without nodes.



iv. Consider the following student statements about the circuits above.

Student 1: "When the current reaches the first node in the parallel circuit, it splits evenly between bulbs D and E. I know that the bulbs are equal in brightness to a single bulb and they are also equal in brightness to each other. Therefore the current through battery 2 must be double the amount of current through battery 1."

Student 2: *"I disagree. I know that all batteries have the same current and all bulbs are the same brightness, so the same current flows through each bulb."* Which of the students, if any do you agree with? Explain.

Discuss your answer to part iv with your demonstrator

Section 4: Measurement of current

In this section, we make a series of measurements that will add some quantitative evidence to the student statements shown in the previous section.

i. Use an ammeter to measure the current in a single bulb circuit as shown in Figure 4.1. Write down your measurement below.





ii. In the circuit of Figure 4.2, the ammeter is measuring the current through one of the bulbs in a parallel circuit. On the basis of your observations and measurements, predict the reading on the ammeter.



Figure 4.2: Parallel circuit with ammeter in one of the branches.

Set up the circuit and verify your prediction.

iii. Predict the reading on the ammeter when it is connected to read the current through the battery in a parallel circuit as shown below. Explain briefly





Figure 4.3 Parallel circuit with ammeter

Set up the circuit shown of Figure 4.4, which measures the current through the battery in a parallel circuit.

How does your observation compare to your prediction?





Figure 4.4: Parallel circuit with ammeter.

iv. Compare the current through the battery in the parallel circuit to the current through the battery in the single bulb circuit. Do your measurements support the idea that the current through a battery can be different in different circuits?

v. Which of the student statements in part iv of Section 3 is consistent with your measurements?

What can you infer about the resistance of a parallel circuit as compared to that of a single bulb circuit?



Section 5: Resistance in parallel circuits

In the previous section we have seen that when we add a bulb in parallel to a single bulb circuit the current through the battery increases. We now carry out more experiments to investigate the properties of parallel circuits.



Figure 5.1: A black box circuit.

Figure 5.2 A two bulb series circuit

i. Consider the circuit shown at in figure 5.1. The black box represents an arrangement of circuit elements. A change is made within the black box and as a result the brightness of the indicator bulb A increases. What can you infer about the change in resistance of the circuit after the connections in the box have been changed?

ii. Set up a two bulb series circuit (figure 5.2). We call bulb A an **indicator bulb** as, throughout this experiment, it indicates the current through the battery.

Suppose that you added a third bulb, C, in parallel with bulb B as shown in figure 5.3.





Do you expect the brightness of bulb A to change when bulb C is added? Explain briefly

Predict how the brightness of the bulbs in the diagram of Figure 5.3 would rank from greatest to least. Carefully explain how you used your model to make your prediction.
iii. Now add bulb C in parallel to bulb B as shown in Figure 5.3. How does the brightness of the indicator bulb A change?

iv. Considering your answer to question i, what can you infer about the change in the resistance of the circuit as bulb C is added in parallel to bulb B?

Is your answer consistent with what you found in Section 3 when you added a bulb in parallel with a single bulb? Explain briefly.

v. Revise the third rule so that it describes how the current through the battery changes when a bulb is added in parallel or in series to a circuit. Include the concept of resistance in your rule. Make sure you rule incorporates the results from Sections 4 and 5.

Check your rule with your demonstrator

Section 6: Voltage

i. Set up a single bulb circuit with the power supply switch at 3 V, 6 V and 9 V, and describe any changes in bulb brightness.

| |
|------|
| |
| |
| |



Figure 6.1 Single bulb circuit

How is the way that the brightness is produced in this case different from the way adding more bulbs to a circuit changes the brightness?

Section 7: Volmeter



We introduce another circuit element, called a **voltmeter**. A voltmeter measures a quantity known as voltage which is related to the ability of a battery or power supply to push/drive current around the circuit. The voltmeter must be connected in parallel to the element which you are measuring, as shown in Figure 7.1

WARNING: When it is not clear which way to connect the voltmeter leads, connect just one lead, then tap the second lead in place to make a fleeting contact while you are watching the meter. If the needle jumps the wrong way, reverse the leads.

Use the voltmeter to measure the voltage across the power supply as shown in the diagram below. Note the reading on the voltmeter.



Voltage:

Disconnect the voltmeter and then add a second bulb in series to the circuit. Reconnect the voltmeter across the power supply as shown below.



Fill in the "series" column of the table below

| Voltmeter Position | Reading for Series Circuit | Prediction for Parallel Circuit |
|---------------------|----------------------------|------------------------------------|
| Across power supply | V | V |
| Across Bulb A | V | V |
| Across Bulb B | V | V |

Repeat the experiment for a two-bulb parallel circuit. Be sure to disconnect from the power supply every time you change the bulb circuit. Fill in the final column of the table. Explain your observations

Explain your observations for the series circuit. On the basis of your observations, is it correct to say that bulb brightness is an indicator of the voltage across the bulb?

| Student Name: | |
|-------------------|--|
| Lab Partner Name: | |
| Lab Date/Time: | |

Student Number: Demonstrator Name

What should I expect in this experiment?

This experiment introduces you to some key concepts concerning rotational motion. These are: torque (τ), angular acceleration (α), angular velocity (ω), angular displacement (θ) and moment of inertia (*I*). They are the rotational analogues of force (F), acceleration (a), velocity (v), displacement (s) and mass (m), respectively.

Pre-lab assignment

What is the angular velocity of a spinning disk that completes 2 full revolutions in 10 seconds?

Introduction:

The equations of motion with constant acceleration are similar whether for linear or rotational motion:

| Linear | Rotational | |
|---|--|------|
| $v_{average} = \frac{s_2 - s_1}{t_2 - t_1}$ | $\omega_{average} = \frac{\theta_2 - \theta_1}{t_2 - t_1}$ | Eq.1 |
| $v_{average} = \frac{v_1 + v_2}{2}$ | $\omega_{average} = \frac{\omega_1 + \omega_2}{2}$ | Eq.2 |
| $v_2 = v_1 + at$ | $\omega_2 = \omega_1 + \alpha t$ | Eq.3 |
| $s_2 = v_1 t + a t^2 / 2$ | $q_2 = W_1 t + \frac{\partial t^2}{2}$ | Eq.4 |

Furthermore, just as a force is proportional to acceleration through the relationship F=ma, a net torque changes the state of a body's (rotational) motion by causing an angular acceleration.

 $\tau = I\alpha$ (Eq.5)

The body's moment of inertia is a measure of resistance to this change in rotational motion, just as mass is a measure of a body's resistance to change in linear motion. The equation $\tau = I\alpha$ is the rotational equivalent of Newton's 2nd law F = ma.

You will use two pieces of apparatus to investigate these equations. The first lets you apply and calculate torque, measure angular acceleration and determine an unknown moment of inertia, *I* of a pair of cylindrical weights located at the ends of a bar. The second apparatus lets you investigate how *I* depends on the distribution of mass about the axis of rotation and lets you determine the value of *I*, already measured in the first part, by a second method. You can then compare the results you obtained from the two methods.

<u>Investigation</u> 1: To measure the moment of inertia, I, from the torque and angular acceleration.

Place cylindrical masses on the bar at their furthest position from the axis of rotation. The bar is attached to an axle which is free to rotate. The masses attached to the line wound around this axle are allowed to fall, causing a torque about the axle



The value of the torque caused by the falling masses is $\tau = Fr$ where *F* is the weight of the mass attached to the string and *r* is the radius of the axle to which it is attached. Calculate the value of τ .

| Mass, m attached to string (kg) | |
|----------------------------------|--|
| Force, F = m . g (N) | |
| Radius, r of axle (m) | |
| Torque, $\tau = F \times r$ (Nm) | |

In this session, you will calculate the <u>angular velocity</u>, ω , and the <u>angular acceleration</u>, α . Distinguish between these two underlined terms.

Wind the string attached to the mass around the axle until the mass is close to the pulley. Release it and measure the time for the bar to perform the first complete rotation, the second complete rotation, the third, fourth and fifth rotation. Estimate your experimental uncertainties.

| Number | | |
|-----------|---------|----------|
| of | θ (rad) | Time (s) |
| Rotations | | |
| 0 | 0 | 0 |
| 1 | | |
| 2 | | |
| 3 | | |
| 4 | | |
| 5 | | |

Since you have the angular distance travelled in a given time you can use Eq. 4 to find the angular acceleration α . Explain how you can do this and find a value for α .



Using Eq.1, calculate the average velocity, $\mathcal{O}_{average}$, during each rotation and fill in the table below.

If angular acceleration is constant, then $\mathcal{O}_{average}$ is equal to the instantaneous velocity at the time half-way between the start and the end of a rotation, t_{mid} . Can you understand this? Explain.

Enter the values in the table below and <u>make a plot</u> of $\mathcal{O}_{average}$ on the y-axis against t_{mid} on the x-axis.

| Number of Rotation | $\mathcal{O}_{average} $ (rad / s) | t _{mid} (s) |
|--------------------------|------------------------------------|----------------------|
| 1 | | |
| 2 | | |
| 3 | | |
| 4 | | |
| 5 | | |

Since this graph gives the instantaneous velocity at a given time, Eq. 3 can be used to find the angular acceleration, α .

What value do you get for α ?



Now you know τ and $\alpha,$ so work out / from Eq. 5.



Create your graph of $\mathcal{O}_{average}$ on the y-axis against t_{mid} on the x-axis.

Do the following plot by hand on this page, or, use JagFit (see back of manual) and attach your printed graph to this page. Important: take care to label axes correctly and include units. *Note, your tutor will account for fitting where done by hand.*



<u>Investigation 2:</u> To determine how the moment of inertia, I, depends on the distribution of mass in a body.

Take the metal bar on the bench and roll it between your hands. Now hold it in the middle and rotate it about its centre so that the ends are moving most. Which is easier? Which way does the bar have a higher value of *I*?



Attach the weights and the bar to the rotational apparatus known as a **torsion axle**. This consists of a vertical axle connected to a spring which opposes any departure from the angle of rotational equilibrium.

Note: The apparatus is delicate. So as not to damage the spring, please keep the rod to within half a rotation from equilibrium.



When you rotate the bar, the spring causes a torque about the axis of rotation which acts to restore the bar to the equilibrium angle. Usually the bar overshoots, causing an oscillation to occur. This is exactly analogous to the way a mass on a linear spring undergoes simple harmonic motion. The period of the oscillations, *T*, is determined by the restoring torque in the spring, *D*, and the moment of inertia, *I*, of the object rotating, in this case the bar and cylindrical weights. They are related by:

$$T = 2\pi \sqrt{\frac{I}{D}}$$



The value of D is written on each torsion axle. Note it here.

To investigate the influence of mass distribution vary the position of the cylinders along the torsion bar, measure the period of oscillation, T, and use the equation above to calculate the moment of interia, I for the combined system of cylinders plus rod. (To improve the precision with which you measure T take the average over 10 oscillations.)

| <i>r</i> – Position of the cylinders along rod (m) | <i>T</i> – Period of oscillation (s) | / for the combined system of cylinder + bar (kgm ²) | <i>I</i> for the cylinders (kgm ²) |
|--|--------------------------------------|---|--|
| 0.05 | | | |
| 0.10 | | | |
| 0.15 | | | |
| 0.20 | | | |
| 0.25 | | | |

Just as you can simply add two masses together to get the total mass (e.g. if the mass of a cylinder is 0.24kg and the mass of a bar is 0.2kg, then the mass of cylinder plus bar is 0.44kg) you can also add moments of inertia together. Given that the moment of inertia of the bar is 0.00414 kgm⁻², will let you fill in the fourth column in the table above.

Plot the value of $I_{cylinder}$ against the position *r*.

Plot the value of $I_{cylinder}$ against the position r^2 .

What do you conclude?

Create a graph of $I_{cylinder}$ against the position, *r*.

Do the following plot by hand on this page, or, use JagFit (see back of manual) and attach your printed graph to this page. Important: take care to label axes correctly and include units. *Note, your tutor will account for fitting where done by hand.*



Create a graph of $I_{cylinder}$ against the position, r^2 . Do the following plot by hand on this page, or, use JagFit (see back of manual) and attach your printed graph to this page. Important: take care to label axes correctly and include units. *Note, your tutor will account for fitting where done by hand*.



The last measurement in the table above, with r = 0.25m, returns the bar + cylinders system to the orientation used in your first investigation. You have thus measured the moment of inertia of the bar + cylinder system in two independent ways. Write down the two answers that you got.

| I from investigation 1: | |
|-------------------------|--|
| I from investigation 2: | |

How do the two values compare? Which is more precise?

Graphing

Many of the experiments in the 1st Year laboratory involve the plotting of a graph. Graphs are very important in Physics as they provide a rich display of the results obtained in an experiment. One third of the human brain is devoted to images, and so we are well optimised to interact with graphs rather than with tables of numbers.

Plotting graphs by hand:

- (1) *Scale:* It is important to choose the scales so as to make full use of the squared page. The scale divisions should be chosen for convenience; that is, one unit is either 1, 2 or 5 times a power of ten e.g. 0.5, 5, 100 etc., but never 3, 7, 9 etc.
- (2) Marking the points: Readings should be indicated on the graph by a ringed dot \otimes and drawn with <u>pencil</u>, so that it is possible to erase and correct any unsatisfactory data.
- (3) Joining the points: In the case of a straight line which indicates a direct proportion between the variables, the ruler is positioned so that the line drawn will pass through as many points as possible. Those points which do not lie on the line should be equally distributed on both sides of the line. A point which lies away from this line can be regarded as 'doubtful' and a recheck made on the readings. In the case of a curve, the individual experimental points are <u>not</u> joined with straight lines but a smooth curve is drawn through them so that as many as possible lie on the curve.
- (4) *Units:* The graph is drawn on squared page. Each graph should carry title at the top e.g. Time squared vs. Length. The axes should be labelled with the name and units of the quantities involved.
- (5) In the case of a straight-line graph, the equation of the line representing the relationship between the quantities *x* and *y* may be expressed in the form

y = mx + c

where m is the slope of the line and c the intercept on the y-axis. The slope may be positive or negative. Many experiments require an accurate reading of the slope of a line.

Using JagFit

In the examples above we have somewhat causally referred to the **'best fit'** through the data. What we mean is, the curve which comes closest to the data points having due regard for the experimental uncertainties.

We can judge this really quite well by eye, but to so isn't quantitative or reproducible between people necessarily, and so doing this manually isn't always the best way.

We can determine a straight line fit to data that varies due to random fluctuations using so-called 'least square fitting', but this requires a calculator/computer and sufficiently large data sets. At least 10 measurements are required to be usefully quantitative in this way, and more typically more than 30 measurements are needed.

A computer can make a difference where data sets are large enough then, and a plotting program called Jagfit is installed on the computers. Jagfit is freely available for download from this address:

http://www.southalabama.edu/physics/software/software.htm



If you are to use it, then double-click on the JagFit icon to start the program. The working of JagFit is fairly intuitive. Enter your data in the columns on the left.

- Under <u>Graph</u>, select the columns to graph, and the name for the axes.
- Under <u>Error Method</u>, you can include uncertainties on the points.
- Under <u>Tools</u>, you can fit the data using a function as defined under <u>Fitting Function</u>. Normally you will just perform a linear fit.

Three of the experiments in this manual were initially developed by the Physics Education Group, CASTeL, Dublin City University.