

Physics Laboratory Manual

PHYC 10180
Physics for Ag. Science
2017-2018



Name.....

Partner's Name

Demonstrator

Group

Laboratory Time

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Introduction

Physics is an experimental science. The theory that is presented in lectures has its origins in, and is validated by, experiment.

Laboratories are staged through the semester in parallel to the lectures. They serve a number of purposes:

- ***an opportunity, as a scientist, to test theories by conducting meaningful scientific experiments;***
- ***a means to enrich and deepen understanding of physical concepts presented in lectures;***
- ***an opportunity to develop experimental techniques, in particular skills of data analysis, the understanding of experimental uncertainty, and the development of graphical visualisation of data.***

Based on these skills, you are expected to present experimental results in a logical fashion (graphically and in calculations), to use units correctly and consistently, and to plot graphs with appropriate axis labels and scales. You will have to draw clear conclusions (as briefly as possible) from the experimental investigations, on what are the major findings of each experiment and whether or not they are consistent with your predictions. You should also demonstrate an appreciation of the concept of experimental uncertainty and estimate its impact on the final result.

Some of the experiments in the manual may appear similar to those at school, but the emphasis and expectations are likely to be different. Do not treat this manual as a 'cooking recipe' where you follow a prescription. Instead, understand what it is you are doing, why you are asked to plot certain quantities, and how experimental uncertainties affect your results. It is more important ***to understand and show your understanding*** in the write-ups than it is to rush through each experiment ticking the boxes.

This manual includes blanks for entering most of your observations. Additional space is included at the end of each experiment for other relevant information. All data, observations and conclusions should be entered in this manual. Graphs may be produced by hand or electronically (details of a simple computer package are provided) and should be secured to this manual.

There will be six 2-hour practical laboratories in this module evaluated by continual assessment. Note that each laboratory is worth 5% so each laboratory session makes a significant contribution to your final mark for the module. Consequently, attendance and application during the laboratories are of the utmost importance. At the end of each laboratory session, your demonstrator will collect your work and mark it.

Laboratory Schedule

Please consult the lab notice board contact the lab manager, Thomas O'Reilly (Science East Room 1.41) to see which of the experiments you will be performing each week. This information is also summarized below.

Timetable: Wednesday 2-4: Groups 1,3,5, and 7
 Wednesday 4-6: Groups 2,4,8,10 and 11
 Friday 3-5: Groups 6 and 9.

Semester	Room		
Week	Science East 143	Science East 144	Science East 145
1	Springs: 1,2	Springs: 3,4	Springs: 5,6
2	Springs: 7,8	Springs: 9,10	Springs: 11
3	Gas: 1,2	Newton 2: 3,4	Heat Capacity: 5,6
4	Gas: 7,8	Newton 2: 9,10	Heat Capacity: 11
5	Gas: 5,6	Newton 2: 1,2	Heat Capacity: 3,4
6	Gas: 11	Newton 2: 7,8	Heat Capacity: 9,10
7	Gas: 3,4	Newton 2: 5,6	Heat Capacity: 1,2
8	Gas: 9,10	Newton 2: 11	Heat Capacity: 7,8
9	Rotation: 1,2	Archimedes: 3,4	Fluids: 5,6
10	Rotation: 7,8	Archimedes: 9,10	Fluids: 11
11	Rotation: 5,6	Archimedes: 1,2	Fluids: 3,4
12	Rotation: 11	Archimedes: 7,8	Fluids: 9,10

Grading Process

Grading is an important feedback for students and as such this is staged through the semester in close synchronisation with the labs. Students benefit from this feedback for continuous improvement through the semester. This is the grading process:

1. A lab script is graded and returned to the student in the subsequent scheduled lab slot.
2. Students resolve concerns regarding their grade with the demonstrator either during or immediately after this lab slot.
3. Grades are preliminary but can be expected to count towards a module grade once visible online. A grade is visible online within two weeks of the graded script being returned.

If the above doesn't happen, it is the student responsibility to resolve this with the demonstrator as early as possible.

Lab Rules

1. No eating or drinking
2. Bags and belongings should be placed on the shelves provided in the labs
3. Students must have their lab manual with them and bring any completed pre-lab assignments to the lab
4. It is the student's responsibility to attend an originally assigned lab slot. Zero grade is assigned by default for no attendance at this lab.

In the case of unavoidable absence, it is the student's responsibility to complete the lab in an alternative slot as soon as possible. The student is graded if doing so, however such a slot can't be guaranteed as lab numbers are strictly limited. The lab manager, Thomas O'Reilly (Room Science East 1.41), may be of help in discussing potential alternative lab times. Where best efforts have been made to attend an alternative but this still hasn't been possible, students should then discuss with their module coordinator.

5. Students work in pairs in the lab, however students are reminded that reports should be prepared individually and should comply with UCD plagiarism policy (see next page).

UCD Plagiarism Statement

(taken from http://www.ucd.ie/registry/academicsecretariat/docs/plagiarism_po.pdf)

The creation of knowledge and wider understanding in all academic disciplines depends on building from existing sources of knowledge. The University upholds the principle of academic integrity, whereby appropriate acknowledgement is given to the contributions of others in any work, through appropriate internal citations and references. Students should be aware that good referencing is integral to the study of any subject and part of good academic practice.

The University understands plagiarism to be the inclusion of another person's writings or ideas or works, in any formally presented work (including essays, theses, projects, laboratory reports, examinations, oral, poster or slide presentations) which form part of the assessment requirements for a module or programme of study, without due acknowledgement either wholly or in part of the original source of the material through appropriate citation. Plagiarism is a form of academic dishonesty, where ideas are presented falsely, either implicitly or explicitly, as being the original thought of the author's. The presentation of work, which contains the ideas, or work of others without appropriate attribution and citation, (other than information that can be generally accepted to be common knowledge which is generally known and does not require to be formally cited in a written piece of work) is an act of plagiarism. It can include the following:

1. Presenting work authored by a third party, including other students, friends, family, or work purchased through internet services;
2. Presenting work copied extensively with only minor textual changes from the internet, books, journals or any other source;
3. Improper paraphrasing, where a passage or idea is summarised without due acknowledgement of the original source;
4. Failing to include citation of all original sources;
5. Representing collaborative work as one's own;

Plagiarism is a serious academic offence. While plagiarism may be easy to commit unintentionally, it is defined by the act not the intention. All students are responsible for being familiar with the University's policy statement on plagiarism and are encouraged, if in doubt, to seek guidance from an academic member of staff. The University advocates a developmental approach to plagiarism and encourages students to adopt good academic practice by maintaining academic integrity in the presentation of all academic work.

UCD Physics Laboratory: Investigation of Springs

Student Name: _____ **Student Number:** _____
Lab Partner Name: _____ **Demonstrator Name:** _____
Lab Date/Time: _____

What should I expect in this experiment?

You will investigate how springs stretch when different objects are attached to them and learn about graphing scientific data.

Introduction: Plotting Scientific Data

In many scientific disciplines, and particularly in physics, you will often come across plots similar to those shown here.

Note some common features:

- Horizontal and vertical axes;
- Axes have labels and units;
- Axes have a scale;
- Points with a short horizontal and/or vertical line through them;
- A curve or line superimposed.

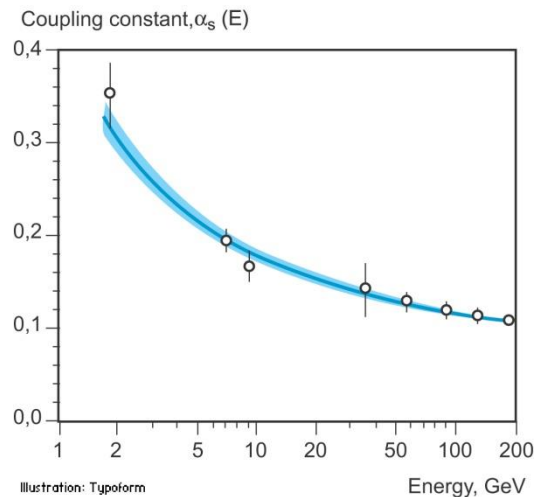
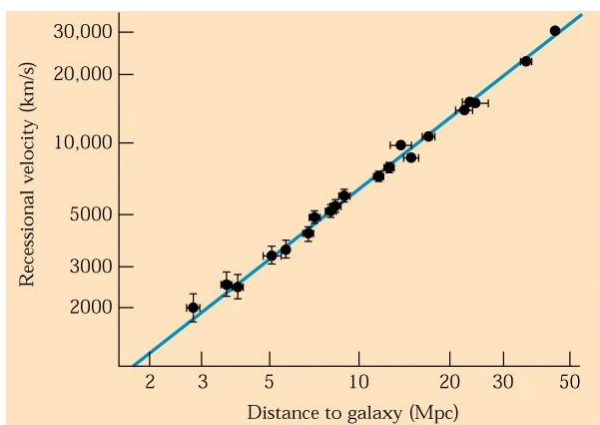
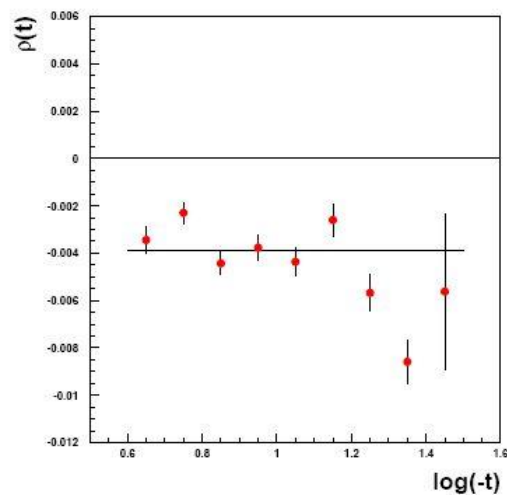


Illustration: Typoform

Why do we make such plots?

What features of the graphs do you think are important and why?

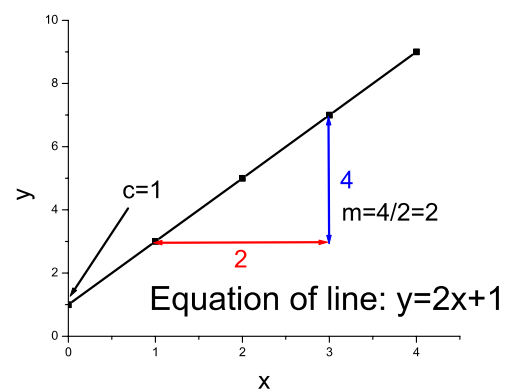
The equation of a straight line is often written as

$$y = m x + c.$$

y tells you how far up the point is, whilst x is how far along the x -axis the point is.

m is the slope (gradient) of the line, it tells you how steep the line is and is calculated by dividing the change in y by the change in x , for the same part of the line. A large value of m , indicates a steep line with a large change in y for a given change in x .

c is the intercept of the line and is the point where the line crosses the y -axis, at $x = 0$.

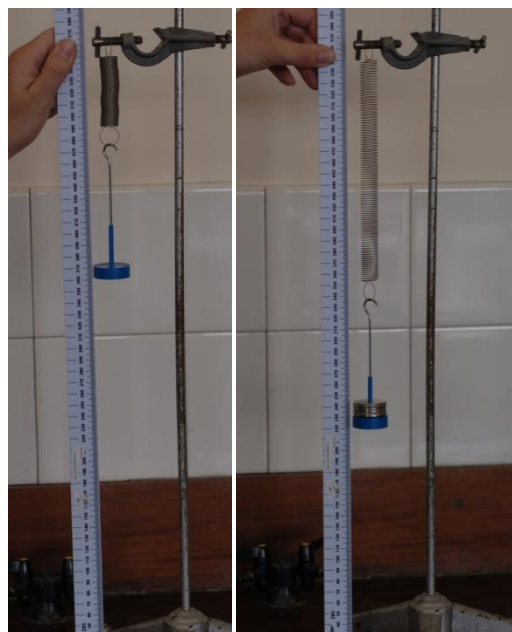


Apparatus

In this experiment you will use 2 different springs, a retort stand, a ruler, a mass hanger and a number of different masses.

Preparation

Set up the experiment as indicated in the photographs. Use one of the two springs (call this one spring 1). Determine the initial length of the spring, be careful to pick two reference points that define the length of the spring before you attach any mass or the mass hanger to the spring. Record the value of the length of the spring below.



Think about how precisely you can determine the length of the spring. Repeat the procedure for spring 2.

Calculate the initial length of spring 1.

Calculate the initial length of spring 2.

Procedure

Attach spring 1 again and then attach the mass hanger and 20g onto the spring. Measure the new length of the spring, using the same two reference points that you used to determine the initial spring length.

Length of springs with mass hanger attached (+ 20 g)

	Spring 1	Spring 2
Position of the top of spring		
Position of the bottom of spring		
New length of spring		

Add another 10 gram disk to the mass hanger, determine the new length of the spring. Complete the table below.

Measurements for spring 1

Object Added	Total mass added to the spring (g)	New reference position (cm)	New spring length (cm)
Disk 1	20		
Disk 2	30		
Disk 3			
Disk 4			
Disk 5			

Add more mass disks, one-by-one, to the mass hanger and record the new lengths in the table above. In the column labelled 'total mass added to the mass hanger', calculate the total mass added due to the disks.

Carry out the same procedure for spring 2 and complete the table below. Use the same number of weights as for spring 1.

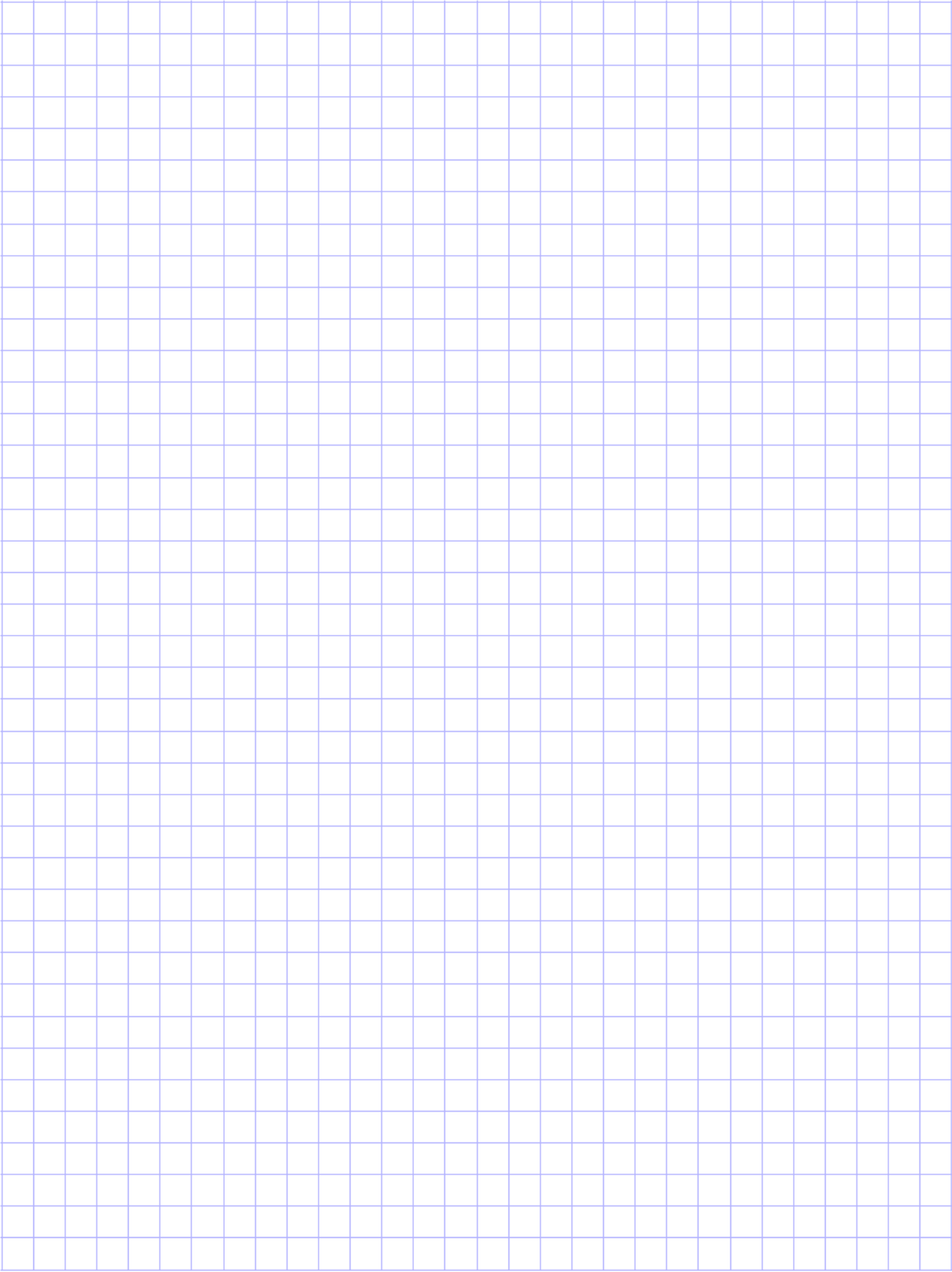
Measurements for spring 2

Object Added	Total mass added to the spring (g)	New reference position (cm)	New spring length (cm)
Disk 1	20		
Disk 2			

Graphical Analysis

Add the data you have gathered for both springs to your graph on the following page. You should plot the length of the spring in centimetres on the vertical y-axis and the total mass added to the hanger in grams on the horizontal axis. Start the y-axis at -10 cm and have the x-axis run from -40 to 100 g. Choose a scale that is simple to read and expands the data so it is spread across the page. Label and give units your axes and include other features of the graph that you consider important.

Plot your graph by hand on this page and make your best estimate for a straight line fit to your data. *Note, your tutor will account for fitting done by hand.*



In everyday language we may use the word 'slope' to describe a property of a hill. For example, we may say that a hill has a steep or gentle slope. Generally, the slope tells you how much the value on the vertical axis changes for a given change on the x-axis.

Algebraically a straight line can be described by $y = mx + c$ where x and y refer to any data on the x and y axes respectively, m is the slope of the line (change in y / change in x), and c is the intercept (where the line crosses the y -axis at $x=0$).

Suppose the data should be consistent with straight lines. Superimpose the two best straight lines, one for each spring, that you can draw on the data points. *Note, your tutor will account for your fitting by hand.*

Examine the graphs you have drawn and describe the 'steepness' of the slopes for spring 1 and spring 2.

Work out the slopes of the two lines.

What are the two intercepts?

How can you use the slopes of the two lines to compare the stiffness of the springs?

In this experiment the points at which the straight lines cross the y-axis where $x = 0$ g (intercepts) correspond to physical quantities that you have determined in the experiment. How well do the graphical and measured values compare with each other?

Look at the graphs on page 7, the horizontal and vertical lines through the data points represent the experimental uncertainty, or precision of measurement in many cases. In this experiment the uncertainty on the masses is insignificant, whilst those on the length measurements are related to how accurately the lengths of the springs can be determined.

How large a vertical line would you consider reasonable for your length measurements?

What factors might explain any disagreement between the graphically determined intercepts and the measurements of the corresponding physical quantity?

The behaviour of the springs in this experiment is said to be “linear”. Looking at your graphs does this make sense?

UCD Physics Laboratory: Investigating the Behaviour of Gases

Student Name: _____ Student Number: _____
Lab Partner Name: _____ Demonstrator Name _____
Lab Date/Time: _____

Goal

You will experimentally investigate the validity of a physical law. After this session, you will have more understanding of the process of experimental verification, and how the law you are testing is relevant to everyday experiences.

Specifically, you will test the Ideal Gas Law relating three variables of Volume, Pressure and Temperature using containers of air. To do this, you will keep one quantity fixed so that you can investigate how two other variables are related. In the first part you will keep the temperature constant and vary the volume to see how the pressure changes. In the second part you will keep the volume constant and vary the temperature to see how the pressure changes.

Warmup exercises

In this laboratory session, we investigate the relationship between the three properties of gases that we can most readily sense: volume, temperature and pressure. We call these macroscopic properties. But we understand that these properties derive from the movement of individual atoms/molecules (microscopic behaviour) that make up a gas, which move randomly, colliding with each other and the sides of the container.

- Pressure, P . The motion of billions of billions of gas particles in a container, causes them to collide with each other and with the sides of their container. In doing so they push on the sides of the container and we measure this as a pressure. For pressure, we use the S.I., unit of a force divided by an area, N/m^2 which is also called the Pascal, Pa.
- Volume, V . A gas is a collection of atoms and/or molecules that expands to fill any container of any shape. For volume, we use the S.I., unit of m^3 .
- Temperature, T . When a container of gas is heated, energy is transferred to the gas from a source of heat. Both the temperature and the internal energy (U) of the gas increase, and we find that $T \propto U$. This internal energy is in the form of a kinetic (motion) energy for the molecules. The molecules move faster as the temperature of a gas increases. Likewise, when a gas is cooled, the molecules slow down.

Using the above information, circle the correct answers below:

If you heat a gas, do the molecules move faster or slower?	faster / slower
If moving faster, do the molecules collide with the container walls more, or less, frequently?	more / less
If the molecules collide more frequently with the container walls, does the pressure increase or decrease?	increase / decrease
If you increase the container volume, are molecular collisions more or less frequent?	more / less
If the molecules collide less frequently, does the pressure increase or decrease?	increase / decrease

Clearly, all three gas properties are interconnected, but how? If we keep one property fixed, we can investigate the relationship between the other two. For example:

- If we keep the gas temperature fixed, we can see how changes in volume affect pressure.
- If we keep the gas volume fixed, we can see how changes in temperature affect pressure.

These two relationships were first investigated by Irish scientist, Robert Boyle (1662), and French chemist, Gay-Lussac (1701). From the above information, can you figure out what remaining relationship was investigated by French scientist, J Charles (1780)?

A relationship between measurable quantities that is demonstrated experimentally and repeated in different ways over many years, can be said to be a physical law. Three scientists proved three relationships between the gas properties, leading to:

- Boyle's Law relating P and V .
- Gay-Lussac's Law relating P and T
- Charles' Law relating V and T

Since these three relationships are interconnected, we can combine them and we call the combined relationship the Ideal Gas Law, which is given by:

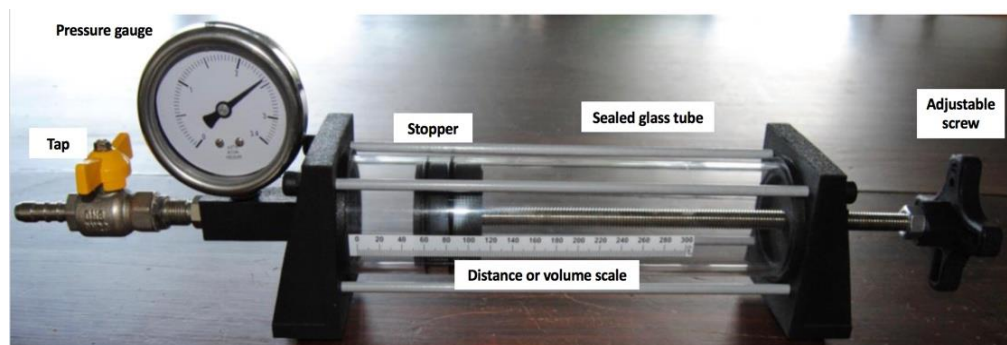
$$PV = nRT$$

where the constant of proportionality is the product of two constants, nR , where n is the number of moles of gas atoms/molecules there are and R is the ideal gas constant. Let's now test these ideas with two experiments.

Experiment 1: How the *pressure* of a gas changes when its *volume* is changed

Apparatus

- A pressure gauge, with a scale in units of pressure i.e. pascals (Pa).
- A sealed glass tube of gas (air), marked with a scale of distance (mm) or volume (ml).



Procedure

- Open the tap (by turning it to a position parallel to the tube). Note the pressure reading. This is your baseline pressure; the pressure of the air all around us.
- Twist the adjustable screw to move the stopper to about a fifth of the way along the tube (as shown in the picture). This is simply a practical starting point for the number of readings to be conducted within the timeframe for the experiment.
- Close the tap to define a fixed amount/mass of gas. Record the baseline pressure.
- Twist the adjustable screw so that the stopper reduces the volume that the gas can occupy within the tube. As you do, notice what happens to the pressure reading. Take readings of pressure as you reduce the volume. (If the tube is marked with units of ml you can write down the volume directly in these units. If the tube is not in these units, you can calculate the volume of the gas by assuming the radius of the tube is 1 cm.)
- Estimate the accuracy of your measurements of volume and pressure.
- Open the tap, to release pressure, and unscrew the stopper to return it to its original position.
- **Note: the equipment is only designed to work up to the maximum pressure on the scale. Keep below this pressure.**

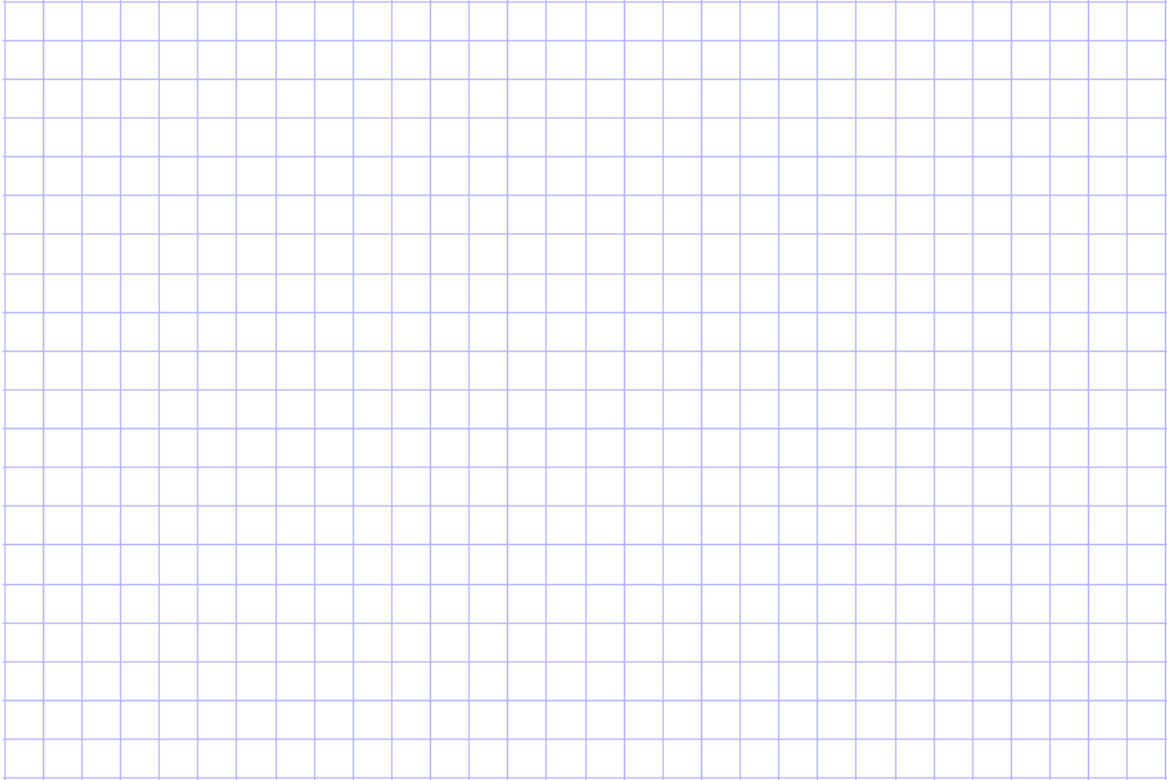
Data

Volume (ml)	Pressure (Pa)

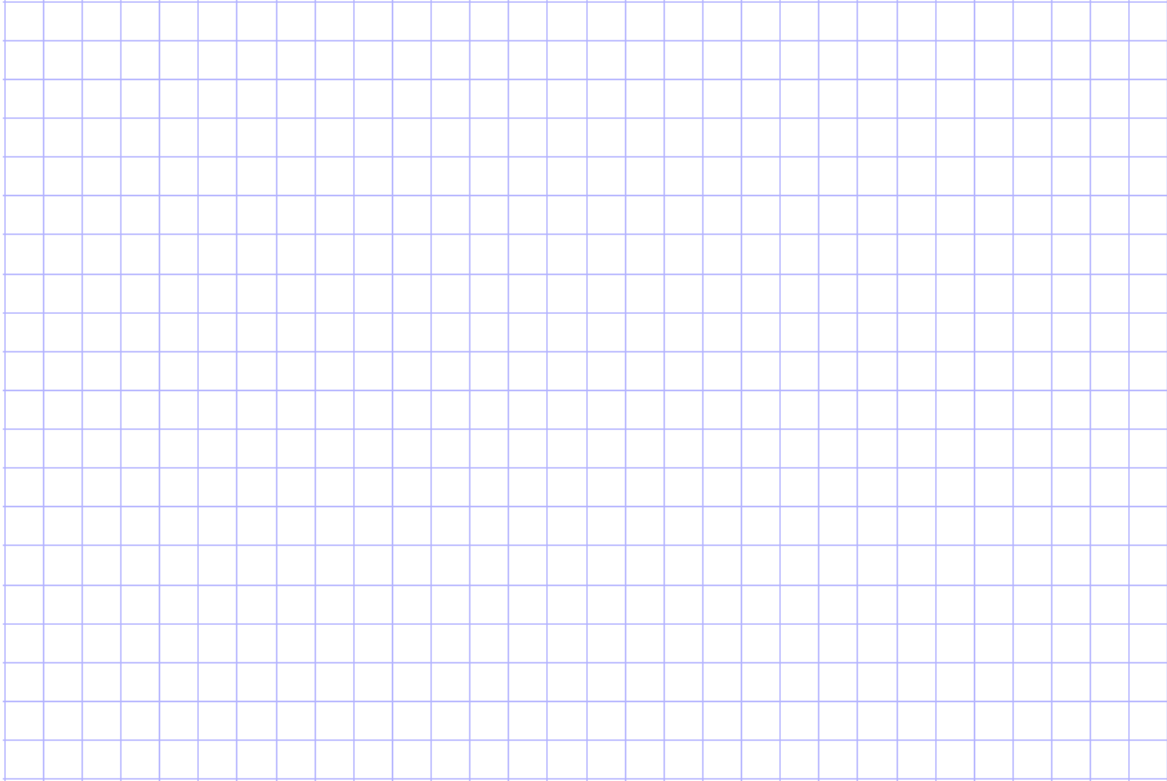
Estimate of error in Volume measurements (ml)	Estimated Error in Pressure measurements (Pa)

Do the following plots by hand on this page, or, use JagFit (see back of manual) and attach your two printed graphs to this page. Important: take care to label axes correctly and include units. *Note, your tutor will account for fitting where done by hand.*

Plot P along the y-axis, as a function of V along the x-axis:



Now plot P along the y-axis, as a function of $1/V$ along the x-axis:



From your graphs, describe how the gas properties are related. Is there a linear relationship between any two variables i.e., does a straight line fit to your points?

A straight-line graph is given by the equation $y = m x + c$, where m is the slope and c is the value of y where the line intercepts the y -axis i.e., where $x = 0$. Determine the slope and the intercept value, c , for your straight-line graph and give these values here, including units.

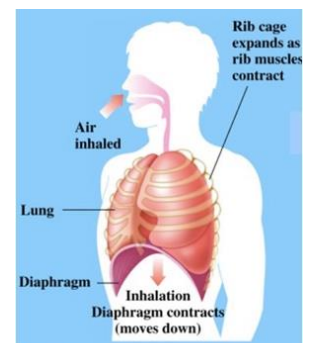
Do you expect the intercept to be at the origin where $P = 0$ and $V = 0$? Explain.

Conclusion

We investigated the relationship between pressure and volume, where temperature is held constant. This is Boyle's Law. From this experiment, briefly state this relationship in your own words and state if this is consistent with the Ideal Gas Law, for which $PV \propto T$.

Implications

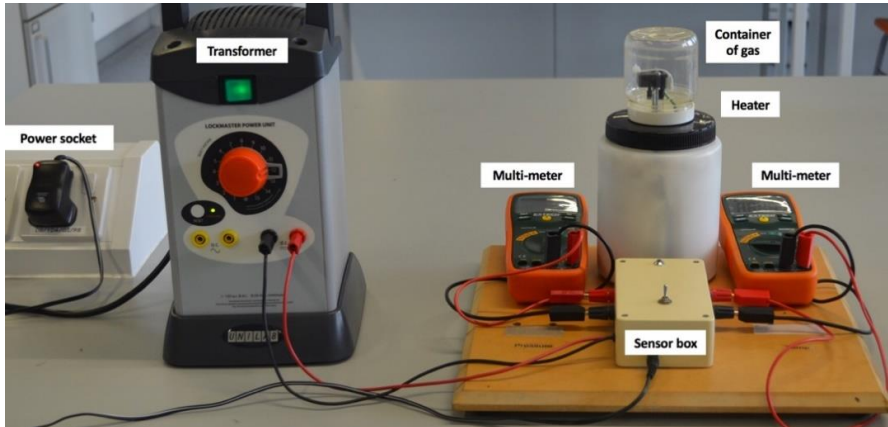
When we inhale, we lower the diaphragm muscle to increase the volume of our lungs. When we exhale, we raise the diaphragm to decrease the volume. Relate this to differences in pressure between the inside and outside of the lungs with the aid of Boyle's Law (the Ideal Gas Law).



Explain another everyday example that relates pressure and volume (for a temperature that's approximately fixed), using the Ideal Gas Law.

Experiment 2: How the *pressure* of a gas change when its *temperature* is changed

Apparatus



- A sealed container of gas (air), connected to a heater.
- A white box containing connections to temperature and pressure sensors.
- Two multi-meters, one to read pressure and one to read temperature.

Procedure

- Ensure all connections are in place (see picture).
- Turn the dial on the “pressure” multi-meter to V (volts), and press the “range” button until it is set to the millivolt (mV) range. You can record mV as a proxy for the units of pressure, Pascals (Pa). Set the “temperature” multi-meter to degrees Celsius (°C).
- Turn on the sensors, by checking that the white box is plugged in and then flipping the switch so that its light comes on. Record the temperature and pressure, as per the multi-meters.
- Turn on the heater, by checking that the large transformer is plugged in and then pressing the large green button so that the button lights up. At this point the gas is being heated and you will notice the temperature readings will slowly increase.
- Take temperature and pressure readings at intervals of about 5 °C until the temperature reaches about 80 °C. Then immediately switch off the heater by pressing the green button.
- Estimate the accuracy of your measurements of temperature and pressure.
- Turn off all equipment, by returning switches to original positions and disconnecting power.

Data

Temperature (°C)	Pressure (Pa)

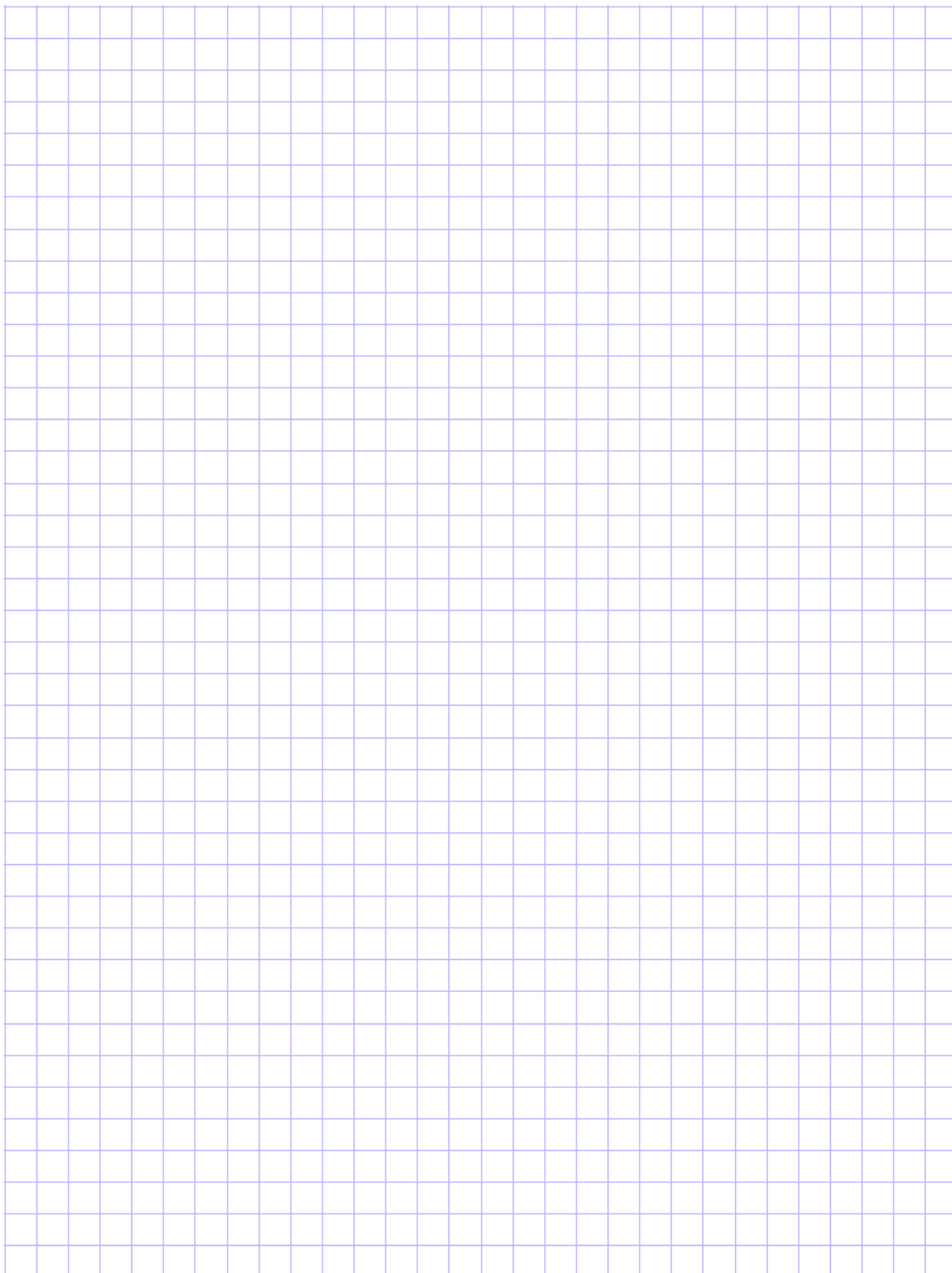
Estimated error in Temperature measurements (°C)	Estimated Error in Pressure measurements (Pa)

Results

Plot pressure, P , (y-axis) as a function of temperature, T in $^{\circ}\text{C}$ (x-axis).

Do this by hand on this page, or, use JagFit (see back of manual) and attach your printed graph to this page. Important: take care to label axes correctly and include units.

Note, your tutor will account for fitting where done by hand.



From your graph, describe how the gas properties of pressure and temperature are related. Is there a linear relationship between any two variables i.e., does a straight line fit to your points?

The curve of a straight-line graph is given by the equation $y = m x + c$, where m is the slope and c is the value of y where the line intercepts the y -axis i.e., where $x = 0$. Determine the slope and the intercept value, c , for your straight-line graph and give these values here, including units.

From your values of m and c , determine the value of temperature in °C for which P would extrapolate to being zero.

Describe what the molecules of the gas would be doing in everyday language at this temperature, T_0 , for which $P = 0$?

Conclusion

We investigated the relationship between pressure and temperature, where volume is held constant. This is Gay-Lussac's Law. From this experiment, briefly state this relationship in your own words.

Explain how your measurements are consistent with the Ideal Gas Law, for which $PV \propto T$.

Implications

Car tyres increase in pressure by $3 \times 10^4 \text{ N/m}^2$ after driving for 20 mins. Explain this with the aid of the Ideal Gas Law

A jam jar can be easier to open after warming it up in a bowl of hot water. Explain this with the aid of the Ideal Gas Law.

Explain another everyday example that relates pressure and temperature (for a volume that's approximately fixed), using the Ideal Gas Law.

UCD Physics Laboratory: Investigation of Acceleration

Student Name: _____ Student Number: _____
Lab Partner Name: _____ Demonstrator Name _____
Lab Date/Time: _____

Goal

You will experimentally investigate the validity of a physical law. After this session, you will have more understanding of the process of experimental verification, and how the law you are testing is relevant to everyday experiences. You do not need prior knowledge of this topic to participate in this laboratory session.

Specifically, you investigate test Newton's 2nd Law, a law relating three variables of force, mass and acceleration, using a cart on a track. It is useful to keep one quantity fixed so that you can investigate how two other variables are related. To do this, you will keep a force fixed along the direction of motion, and relate an acceleration to a mass.

Warmup exercises

Newton's second law is given by the vector relationship, $\vec{F} = m\vec{a}$, for which a force causes an acceleration and the constant of proportionality is mass, m . However, for motion confined to a straight line (one dimensional motion), we can simplify this law to the scalar relationship, $F = m a$, where F is the value of the net force acting on an object along its allowed direction of motion, and a is the value of acceleration in this direction of motion. We consider only motion in a straight line in this laboratory and so we are able to use this scalar form of the law.

If you throw a heavy ball with a force F and then throw a light ball with the same force, which ball gathers more speed? _____
heavy/light

Acting under constant acceleration, a cart starts from rest and has a speed of 2 m/s after 5 s. What is the acceleration of the cart? _____

Forces cause acceleration. For example if you kick a ball of mass m with a force ' F ', its acceleration is ' a '; if you then kick the same ball with a force twice as big, ' $2F$ ', then it accelerates at ' $2a$ '. In other words, the acceleration, a , is larger when the force, F , is larger:

$$a \propto F$$

The acceleration is larger when the mass, m , of the object is smaller:

$$a \propto \frac{1}{m}$$

We can combine these two relationships into one:

$$a \propto \frac{F}{m}$$

Isaac Newton (1687) provided experimental evidence of this relationship, and so it became a 'Law'. It is now called Newton's 2nd Law, and is more commonly written as:

$$F = m a$$

The unit of force is kg·m/s² which is called the Newton (symbol N), in honour of Isaac Newton.

If an apple falls from a tree, it speeds up until it hits the ground. So there must be a force which causes this acceleration. The acceleration due to the Earth's gravitational force field has been measured experimentally to be 9.8 m/s². We denote this as '*g*' since its value is always the same, instead of generic acceleration '*a*' (which can have many values). So the gravitational force is the product, *mg*.

To test Newton's 2nd Law, you will keep one quantity fixed so that you can investigate how two other variables are related. Specifically, you will keep the force fixed and relate a horizontal acceleration to a mass which is varied.

Apparatus

- One cart, of mass 0.5 kg
- A low-friction track, with a pulley wheel on one end
- A string, with a disk tied to one end and a hook to the other, threaded over the pulley wheel
- Two photogates connected to a blue data-logger
- Three metal bars, of mass 0.5 kg each, which can be added to the cart to increase its mass

When using a pulley, the string has an equal tension throughout. This simplifies our thinking, because we can consider the stage as being accelerated horizontally due to a constant horizontal force of magnitude, *F*, and we also consider *F* to be the magnitude of force exerted vertically between the string and the hook-mass. We return to this with an equation later.

Experiment: Acceleration from a constant force along a horizontal plane

Experimental set-up

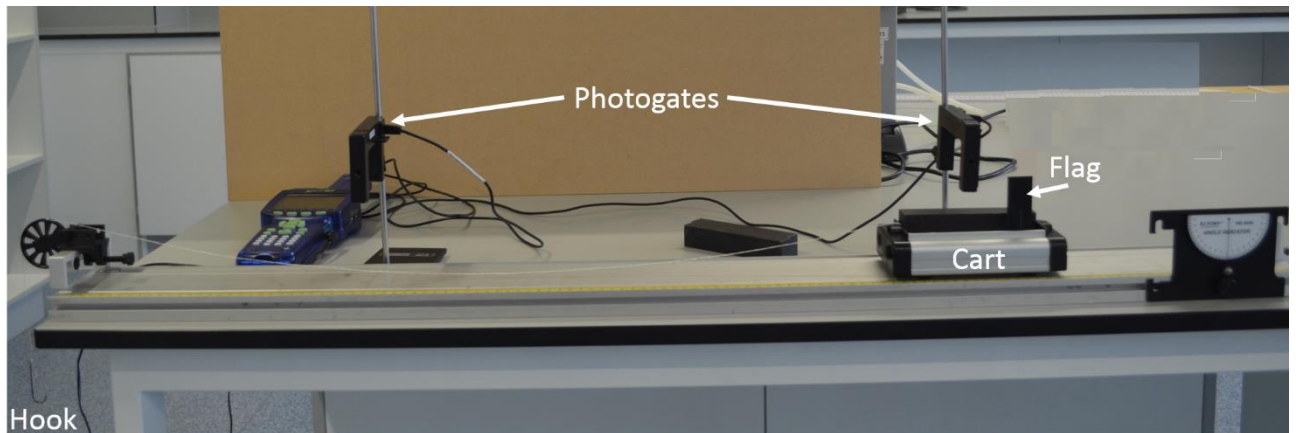


Fig 1

i) Setting up the cart on the track:

- Position the track on the laboratory bench in such a way that the pulley wheel hangs over one end of the bench.
- Ensure the track is level. This is done via an adjustable leg at one end.
- Place the cart on the track at the opposite end to the pulley wheel.
- You will find a string, with a disk tied to one end and a hook to the other. Attach the string to the cart (by simply placing the disk on the cart), and thread the string over the pulley wheel so that the hook hangs down.
- Attach a 10 g mass to the hook, and see how this causes the cart to accelerate along the track.
- Insert the rectangular metal "flag" into the hole at head of the cart, with the largest surface facing you. Make sure the flag is secure and does not move. (This can be achieved by lifting it slightly out of the hole.) The role of the flag is to interrupt the light beam of the photogates (see below).

ii) Setting up the two photogates:

- The photogates comprise an infrared light source on one side, and a detector on the other, fig 2. Infrared light is invisible to the human eye, but is represented by the red line in the figure. When the beam is interrupted it sends a signal to the blue data logger.
- Place the photogates at positions 30 cm and 80 cm on the track. In this way, the distance between the gates is 50 cm.
- In order to calculate acceleration, we must measure the change in velocity in a given time interval.
- The velocity is determined by how long the cart's metal flag takes to move past a given photogate. The photogate is connected to a blue data logger, which reports how long the beam is interrupted for (i.e. time). It then uses the width of the flag (i.e. distance) to estimate the velocity of the cart. For this reason, we must input the width of the flag (or flag length) when we set up the data logger (below). The cart *velocity* is calculated from how long it takes its flag to pass through the photogate beam. To output these results, the blue data logger must be set up correctly (see below).

- The cart *acceleration* is determined by computing the change in velocity between the two photogates.

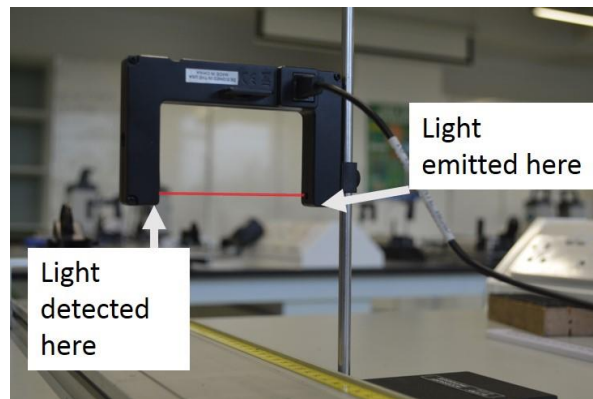


Fig 2

iii) Setting up the blue data-logger:

- Turn on the power supply at the socket. Turn on the blue data-logger. A screen will appear, select “photogate timing” and enter the flag length (0.0250 m) and photogate spacing (0.5000 m) by pressing \checkmark to edit and again to confirm.
- Ensure that only ‘Velocity In Gate’ and ‘Time Between Gates’ are set to visible.
- Then press the home key.
- Press F1 or navigate to the graph section. Once on the graph screen, press F4 to open the graph menu. Navigate to ‘Two Measurements’ and press select.
- Press the select key and navigate to the ‘Y’ (i.e. y-axis), which should be visible on the right-hand side of the graph. Press select and choose ‘Time Between Gates’. This will now appear on the right of the graph. The left axis should already be displaying “Velocity in Gates”.
- You can now record data by pressing \checkmark to begin and stop.
- On the graph screen, velocity will be displayed as a line and the time taken to travel between gates will be displayed as both a single point on the graph and as a numerical value along the right-hand side Y axis of the graph.
- To read the data from your completed run accurately, press F3 and select ‘Smart Tool’. Use the navigation buttons to see the precise values for the points on the graph.
- To save your experimental data, use the arrow keys to highlight your data file in the RAM memory and press “F4 files”. Select the “copy file” option and then choose the external USB as the destination for the file, and press “F1 OK”. Transfer the USB data stick to the lab computer, and create a graph.

Procedure

- On the data-logger, press \checkmark to begin recording data, and again after the cart has completed a run.
- Record the total mass being accelerated (i.e. the mass of the cart, the metal block on the cart, the hook, the additional mass on the hook). Release the cart, and record its velocity and time as it passes each photogate.
- Add a metal bar to the cart to increase its mass, and repeat the above steps.
- Repeat until you have added three metal bars. Be sure that the metal bars are not stacked too high i.e. that they do not trigger the photogate.

Data:

Mass of hook, m_{hook} (kg)	Mass of cart, m_{cart} (kg)	Velocity 1, v_1 (m/s)	Velocity 2, v_2 (m/s)	Time 1, t_1 (s)	Time 2, t_2 (s)	Acceleration, a (m/s ²)

- Calculate the acceleration (i.e. the change in velocity during a given time interval):

$$a = \frac{v_2 - v_1}{t_2 - t_1}$$

- On the blue data-logger, use the arrow keys to highlight your data file in the RAM memory and press “F4 files”. Select the “copy file” option and then choose the external USB as the destination for the file, and press “F1 OK”. Before transferring the USB data stick to the lab computer to create a graph, we must decide what to put on the x and y axes (see below).

Results

If Newton's 2nd Law is indeed, $F = m a$, it will plot as a straight line i.e., it will take the form:

$$y = k x + c$$

where k is the gradient (slope), and c is what we will call the intercept (the value of y where x is zero). Here we refer to k instead of the traditional m for the gradient of a straight line, because we have already used m to mean mass.

In this investigation, we kept the force constant and increased the mass in order to investigate how acceleration changes. Therefore, we put mass on the x-axis and acceleration on the y-axis. How can we rearrange Newton's 2nd Law into the mathematical format of a straight line graph, where the x-axis is the mass and the y-axis is the acceleration?

We could rearrange $F = m a$ into the format $y = k x + c$ as follows:

$$\frac{1}{a} = \frac{1}{F} m$$

where a is acceleration, F is force, m is mass and $c = 0$

We know m is mass, but which mass? (Circle the correct answer below)

- i) $m = m_{cart}$
- ii) $m = m_{hook}$
- iii) $m = m_{cart} + m_{hook}$
- iv) $m = m_{cart} - m_{hook}$

The cart and hook are connected together and so they have the same magnitude of acceleration, a , and the net mass moving is $m_{cart} + m_{hook}$. Thus, we can more usefully rearrange our equation as follows:

$$\begin{aligned}\frac{1}{a} &= \frac{1}{F} (m_{cart} + m_{hook}) \\ &= \frac{1}{F} m_{cart} + \frac{1}{F} m_{hook}\end{aligned}$$

Now, for this case where $\frac{1}{a}$ is the y-axis and m_{cart} is the x-axis, which term is the slope of this graph? And which term is the intercept i.e., the value of y where x is zero?

Plot your experimental data, with $\frac{1}{a}$ as the y-axis and m_{cart} as the x-axis. If the graph is a straight line, then you have verified Newton's 2nd Law.

Plot your graph by hand on this page and make your best estimate for a straight line fit to your data. *Note, your tutor will account for your fitting by hand.*
Important: take care to label axes correctly and include units.



You can now find a value for F in two separate ways and compare them for accuracy, as follows:

From your graph determine the slope, and hence calculate F .

From your graph determine the intercept, and hence calculate F .

Compare your value of F determined in the two different ways above, determine the best value of F and estimate the uncertainty on your resulting value for F .

From the value you found for F , calculate the acceleration due to gravity, g . How does it compare to the generally accepted value of g ?

Hint: because we use a pulley, the force, F also acts vertically on the hook. The vertical motion of the hook can therefore be considered under solely this tension force F and the force due to gravity, $m_{\text{hook}}g$.

Conclusion

We sought to experimentally verify Newton's 2nd Law, $F = m a$.
State Newton's 2nd Law in your own words:

Implications

If you simultaneously drop a bowling ball and a billiard ball, they will hit the ground at the same time. This means that they were both accelerated at the same rate. What is this rate?

Does the bowling ball experience a larger, smaller or the same force as the billiard ball? Use Newton's 2nd Law to justify your answer.

A car of mass, m , is pulled into motion in a straight line by a lorry exerting a force, F on a rope. Assuming no friction, determine the acceleration of the car where the rope is aligned along the same direction as the car's motion.

UCD Physics Laboratory: Investigation of Heat Capacity

Student Name: _____ Student Number: _____
Lab Partner Name: _____ Demonstrator Name: _____
Lab Date/Time: _____

Goal

You will experimentally investigate the validity of a physical law. After this session, you will have more understanding of the process of experimental verification, and how the law you are testing is relevant to everyday experiences. You do not need prior knowledge of this topic to participate in this laboratory session.

Specifically, you will determine and the heat capacity of two metals from measurements you make of their temperature rise on being heated.

Warm-up exercises

Heat can be thought of as the amount of energy flowing from one object to another due to their temperature difference. Heat is given the variable, Q and is given in units of Joules, J. When we heat an object, we increase the object's internal energy and as a result we increase its temperature, T by an amount, ΔT .

Different objects, of different forms and materials, will likely experience different increases in temperature for the same value of heat. We define the Heat Capacity for any particular object as: $Q/\Delta T$.

Which do you think takes more energy? To heat a bath of water from 20 °C to 30 °C, or to heat a cup of coffee from 20 °C to 30 °C? Bath / Coffee

Considering Conservation of Energy, for the same value of ΔT , two identical objects combined will require double the amount of heat as just one of the objects. It takes more heat to increase the temperature of a more massive object, and we find that the heat capacity for an object depends on its mass. To define a property for a material, we use the idea of Specific Heat Capacity, which is the Heat Capacity per kilogram of the material.

Specific Heat Capacity, c is defined as:

$$c = \frac{Q}{m \Delta T}$$

where the heat supplied is Q in units of Joules, the mass is m in units of kg, the temperature change is ΔT in units of degrees Celsius, °C (or equivalently for what is a difference in temperature, in Kelvin, K).

Specific heat capacity is the energy transferred to raise the temperature of a 1 kg object by 1 °C. Maybe a better name for this would have been Specific Energy Transfer, but the name was arrived at before we had a better understand of conservation of energy in thermodynamics.

Write here the units for specific heat capacity, worked out from its definition above:

In this laboratory session, we will add an amount of heat (Q) to a metal sample of known mass (m) and measure the resulting temperature change (ΔT). From this we will calculate the specific heat capacity (c). We will do this for an aluminium and a copper block.

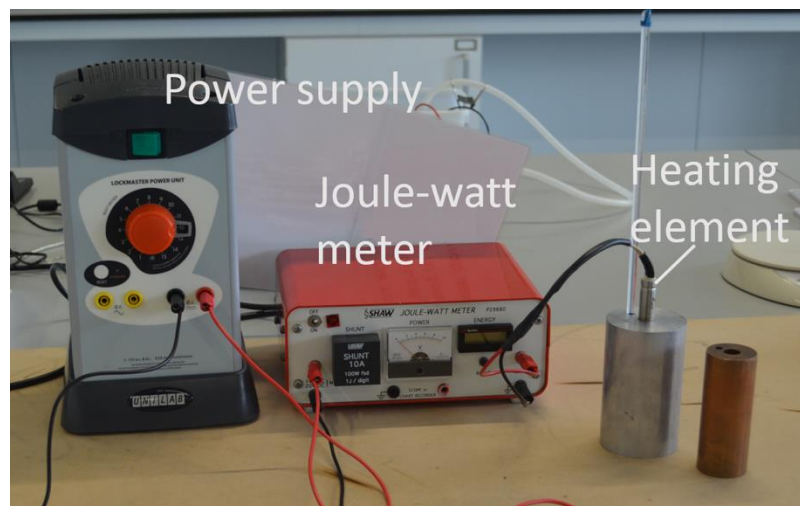
Safety

- Do not place the metal blocks or the heating element directly onto the lab bench. Use insulating mat.
- Take care when handling the metal blocks and the heating element, as they can be hot.
- Switch off all of the apparatus when you have completed the experiment.

Apparatus

- Power supply
- Joule-Watt meter (meter which measures energy)
- Heating element (metal rod/element which inserts into the centre of the metal blocks)
- Aluminium block, 1kg
- Copper block, 1 kg
- Thermometer
- Stop-watch

Experiment: Measuring the heat capacity of two metals, aluminium and copper



Experimental Set-up

We will use electricity to generate heat. As current flows through the heating element, its temperature increases.

- Place the heating element into the central hole of the metal block (start with the aluminium block).

We then need to connect the heating element to the power supply. However, to measure the amount of heat energy generated (Joules), we must include a Joule meter in our circuit also.

- Connect the positive (red) and negative (black) sockets of the Joule-Watt meter to the positive and negative sockets of power supply.
- Connect the two wires of the heating element to the Joule-Watt meter (where it says 'load'), according to the positive and negative polarity.
- Set the power supply to 12 volts DC.
- Insert the thermometer into the other hole in the metal block, to allow measurement of temperature ($^{\circ}\text{C}$).

Procedure

- Measure the fraction of the length of the heating element which is inserted into the block.
- Record the initial temperature of the block, T_1 , at time $t_1 = 0$.
- Press reset on the Joule-Watt meter and reset the timer.
- Switch on the power supply and start the stop-watch.
- Record the energy supplied to the heating element according to the Joule-Watt meter.
- Scale the Joule-Watt meter reading, E , according to the fraction of the heating element inserted in the block, f , to get the heat energy transferred to the block, Q i.e., $Q = f E$. Record these fractions here:

	Fraction of element inserted, f
Aluminium	
Copper	

- Record the temperature at one minute intervals, until the temperature has risen by 20 degrees or after 20 minutes, whichever comes first. This is time, t_1
- Switch off the power supply and wait for the temperature to begin to lower. Then begin recording measurements of the temperature as a function of time (starting from what we will call t_2) as the block cools.

Data

Record your data on the following page

Aluminium, Al		
Time, t (minutes)	Heat transferred, $Q = f E$ (J)	Temp, T (°C)
Heating		
0 (t_0)		
1		
2		
3		
4		
5		
6		
7		
8		
9		
10		
11		
12		
13		
14		
15		
16		
17		
18		
19		
20 (t_1)		
Cooling (no heating)		
Time, t (minutes)	X	Temp, T (°C)
0 (t_2)		
1		
2		
3		
4		
5		
6		
8		
10		
12		
14		
16		

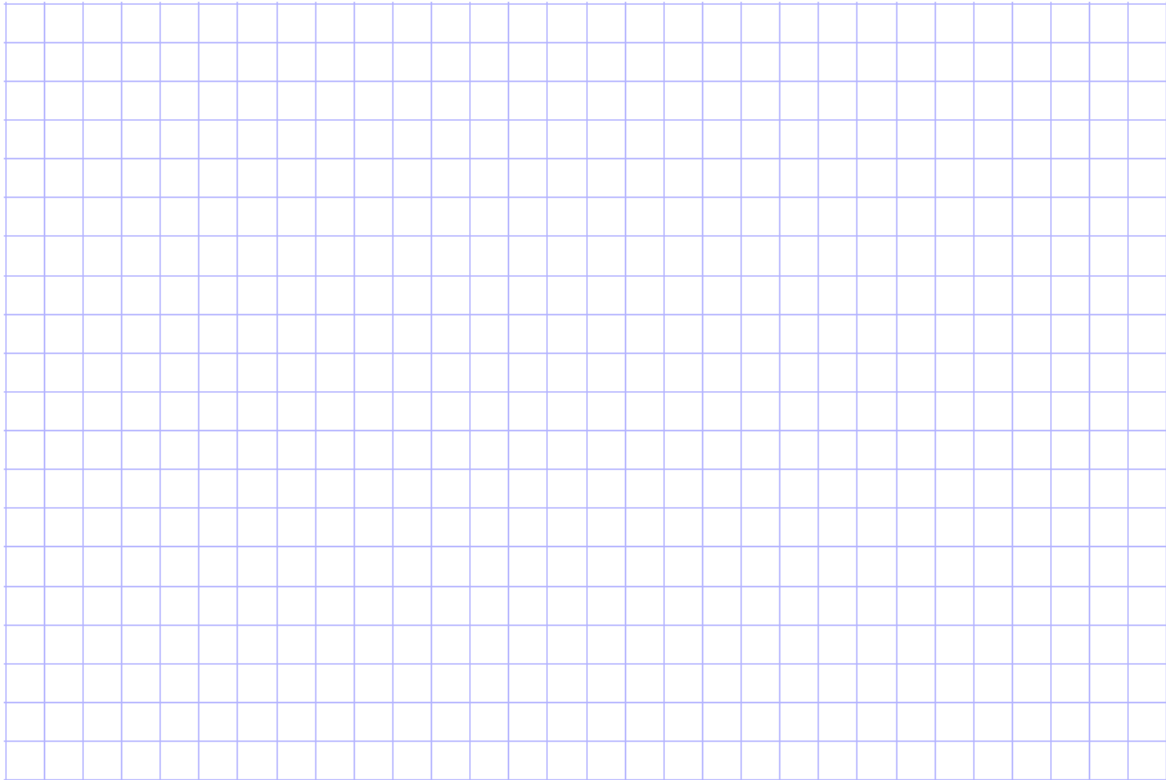
Copper, Cu		
Time, t (minutes)	Heat transferred, $Q = f E$ (J)	Temp, T (°C)
Heating		
0 (t_0)		
1		
2		
3		
4		
5		
6		
7		
8		
9		
10		
11		
12		
13		
14		
15		
16		
17		
18		
19		
20 (t_1)		
Cooling (no heating)		
Time, t (minutes)	X	Temp, T (°C)
0 (t_2)		
1		
2		
3		
4		
5		
6		
8		
10		
12		
14		
16		

Results

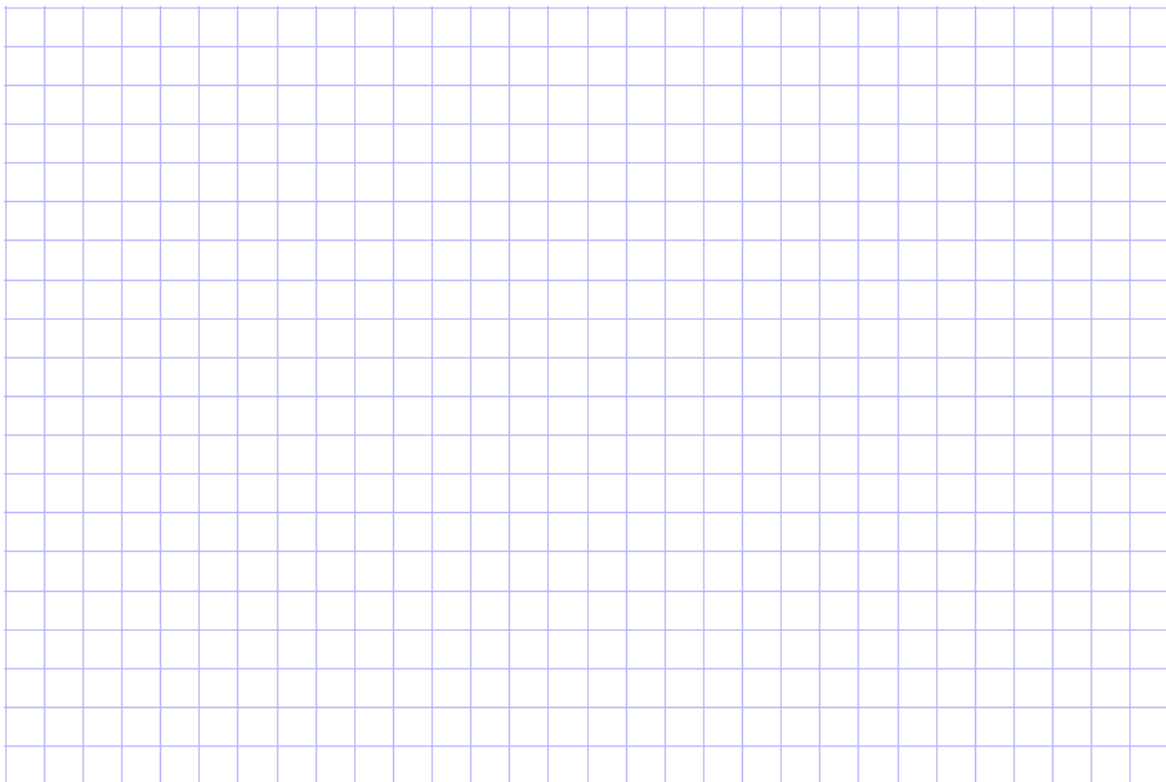
Make plots by hand on the following page, or, use JagFit (see back of manual) and attach your two printed graphs to this page. Label axes correctly and include units.

Note, your tutor will account for fitting done by hand.

a) Plot the temperature difference, $\Delta T = T(t) - T(t_0)$ along the y-axis, as a function of the heat supplied to the block, Q along the x-axis. This is your data from time t_0 to t_1 . Do this for both the Al and the Cu blocks:



b) Now plot temperature, $T(t)$ along the y-axis, as a function of time, t along the x-axis, when the blocks are cooling. This is your data starting from time t_2 . Do this for both the Al and the Cu blocks:



Describe how the parameters, ΔT and Q are related in graph a. Does a straight line fit to your points?

A straight-line graph is given by the equation $y = m x + k$, where m is the slope and k is the value of y where the line intercepts the y -axis i.e., where $x = 0$. On your graphs, determine the slope and the intercept value, k , for your best straight line fits to your Al and Cu points for graph a, and give these values here, including units.

Al:

Cu:

We defined specific heat earlier as: $c = \frac{Q}{m \Delta T}$

What could you expect your gradient, m , to represent in terms of the specific heat capacity, c and the mass, m ?

From this, calculate the specific heat capacity of the two metals, and compare them to the theoretical values.

Metal	Specific Heat Capacity, measured ($\text{J kg}^{-1} \text{ }^\circ\text{C}^{-1}$)	Specific Heat Capacity, theoretical ($\text{J kg}^{-1} \text{ }^\circ\text{C}^{-1}$)
Aluminium		960
Copper		385

If your results do vary from the theoretical values, this may be due to heat transfers out of the block via conduction, Q_c , to air which then takes away the heat by convection (moving away with the heat) and to the table. It may also be due to heat transfers out of the block via radiative cooling (the giving off of far-infrared light), Q_r .

Draw or fit curves to your data for Cu and Al in graph b, and from inspection of these graphs, give your best estimate here of heat loss during the experiment for the Cu and the Al. Give your reasoning here too:

What percentage of heat was lost from the block to cooling relative to the heat that was transferred to the block by the element, this while the element was switched on i.e., between times t_0 and t_1 ?

What would you argue is the dominant physical mechanism for heat loss in this experiment? Explain this by referring to the following hints.

Hints:

- i) For conduction cooling, Q_c , it is possible to derive that $Q_c \propto \Delta T$, where ΔT
- ii) For radiative cooling, Q_r , it is possible to derive that: Q_c is approximately constant over the range of temperatures in this experiment.
- iii) which of these mechanisms would best explain any deviation from a straight line behaviour in graph a?
- iv) which of these two mechanisms would best explain curve fits to your data in graph b.
- v) are both mechanism required to explain you results?

Conclusions

In this experiment, we explored the relationship between heat and temperature:

$$c = \frac{Q}{m \Delta T}$$

and we measured the specific heat capacity, c for two metals.

The words, 'heat' and 'temperature' are often confused in everyday life. We might hear it said that the 'fridge door was opened and the cold got out', or 'the water in the kettle contains a lot of heat'. Clearly state what heat, Q , really is:

Implications

1. An electric heater supplies 18 kJ of heat energy to a metal block of mass 0.5 kg. The temperature of the block rises from 20 °C to 100 °C during the heating process. Assuming that very little heat is lost from the block during heating, determine (and explain here) the specific heat capacity of the metal. Can you make a case here for what element this metal is (which forms the Earth's core) by its specific heat capacity?

Ans. 450 J kg⁻¹ °C⁻¹

2. Estimate how much heat energy is required to boil just enough water to make two full cups of tea? Let's say a full cup is 250 ml.

Ans. about 170kJ

UCD Physics Laboratory: Investigation of Fluid Flow

Student Name: _____ Student Number: _____
Lab Partner Name: _____ Demonstrator Name: _____
Lab Date/Time: _____

Theory

When a fluid moves through a channel of varying width, as in a Venturi apparatus, the volumetric flow rate (volume/time) remains constant but the velocity and pressure of the fluid vary. In the Venturi apparatus there are two different channel widths.

The flow rate, Q , of the fluid through the tube is related to the speed of the fluid (v) and the cross-sectional area of the pipe (A). This relationship is known as the **continuity equation**, and can be expressed as

$$Q = A_0 v_0 = Av \quad (\text{Eq.1})$$

where A_0 and v_0 refer to the wide part of the tube and A and v to the narrow part. As the fluid flows from the narrow part of the pipe to the constriction, the speed increases from v_0 to v and the pressure decreases from P_0 to P .

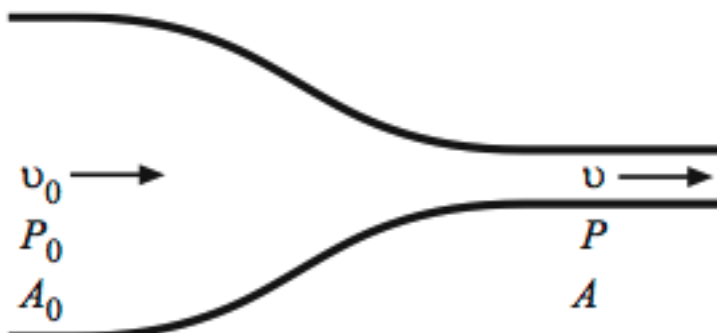


Figure 1: Fluid flow through a pipe of varying diameter

If the pressure change is due only to the velocity change, a simplified version of Bernoulli's equation can be used:

$$P = P_0 - \frac{\rho}{2} \{v^2 - v_0^2\} \quad (\text{Eq. 2})$$

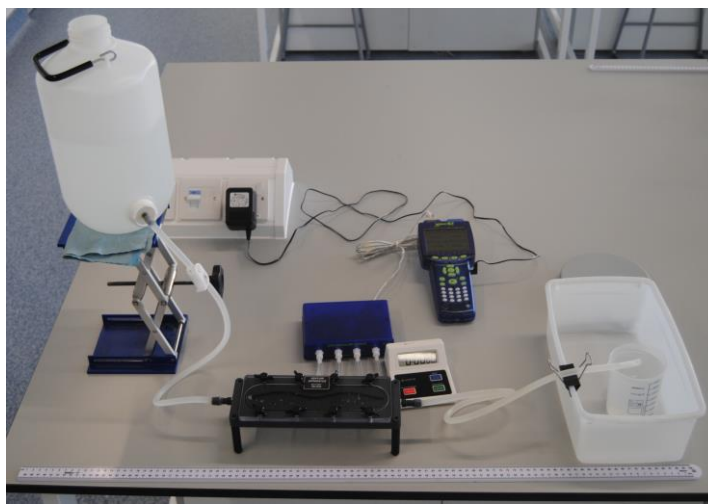
Here ρ is the density of water: 1000 kg/m³.

The flow rate also depends on the pressure, P_0 , behind the fluid flowing into the apparatus. In this experiment the pump provides the pressure that makes the fluid flow through the apparatus. The higher the power to the pump the greater the pressure and the faster the fluid flows.

In this experiment you will use the Venturi apparatus to investigate fluid flow and verify that equation 2 holds. You will also investigate how the voltage supplied to the pump affects the pressure and flow rate.

Apparatus

The apparatus consists of a reservoir, which is a plastic box, of water connected to a Venturi apparatus through which the water can flow into a collecting beaker, itself placed in a box. The electrical pump in the box causes the water flow in the apparatus.



Procedure

Using the spare apparatus in the laboratory, measure the depth of the channel and the widths of the wide and narrow sections. Calculate the large (A_0) and small (A) cross-sections by multiplying the depth by the width for the two sections of the apparatus.

Depth _____ Width(large) _____ Width (narrow) _____
Area (A_0) _____ Area (A) _____

Before putting any water in the apparatus, connect the Venturi apparatus to the Quad pressure sensor and GLX data logger.

1. Connect the tubes from the Venturi apparatus to the Quad Pressure Sensor. Ensure that they are connected in the right order. The one closest to the flow IN to the apparatus is connected to number 1 etc.
2. Connect the GLX to the AC adapter and power it up.
3. Connect the Quad Pressure sensor to the GLX. A graph screen will appear if this is done correctly.
4. Navigate to the home screen (Press "home" key) and then navigate to 'Digits' and press select. Data from two of the four sensors should be visible.
5. To make the data from all four sensor visible press the F2 key. All sensor input should now be visible.
6. Make sure that the eight fixing taps on the Venturi apparatus are all just finger tight. Fill the reservoir so that the pump is fully submerged in the plastic box. **Ensure that the outlet of the apparatus is in the beaker which is in the box.** Turn on the power supply to the pump and set the voltage to 10V. Remove any air bubbles by gently tilting the outlet end of the Venturi apparatus upwards.
7. Calibrate the sensors, using the atmospheric pressure reading:
 - (i) Press "home" and "F4" to open the sensors screen.
 - (ii) Press "F4" again to open the sensors menu.
 - (iii) From the menu, select "calibrate" to open the calibrate sensors window.
 - (iv) In the first box of the window, select "quad pressure sensor".
 - (v) In the third box of the window, select "calibrate all similar measurements".
 - (vi) In the "calibration type" box, select "1 point offset".
 - (vii) Press "F3", "read pt 1".
 - (viii) Press "F1", "OK".

Measure the time that it takes for 400 ml ($0.4\text{l} = 4 \times 10^{-4} \text{ m}^3$) of water to flow through the Venturi apparatus. Be sure to read the water level by looking at the bottom of the meniscus.

When the flow is steady note the pressures on the four sensors. Enter your data in the table. Repeat the measurements twice more. **Be sure to return all the water to the reservoir (plastic box). Make sure that the apparatus stays free of air bubbles.**

Run	P ₁ /kPa	P ₂ /kPa	P ₃ /kPa	P ₄ /kPa	Time /s
1					
2					
3					
Average					

Calculate the flow rate, Q, volume/time, from the average value of the time taken for 400 ml to flow through the apparatus. $1\text{ml} = 1\text{cm}^3 = 1 \times 10^{-6} \text{ m}^3$.

Use equation (1) and the cross-sectional areas that you calculated to work out the velocity of the water in the wide (v_0) and narrow (v) sections of the apparatus.

$v_0 =$ _____

$v =$ _____

Which is larger v or v_0 , is this what you expected?

If the apparatus was not constricted the pressure at point 2 (P_0) is equal to the average value of P_1 and P_3 . Use your average values of P_1 and P_3 to calculate P_0 :

$P_0 = 1/2(P_1 + P_3)$ _____

Use equation 2 and your values for P_0, v_0 and v to calculate a value for P , the pressure in the narrow section of the apparatus. The SI unit for pressure is the Pascal (Pa), $1\text{kPa} = 1000\text{ Pa} = 1000\text{ N/m}^2 = 1000\text{ kg s}^{-2}\text{ m}^{-1}$.

$P =$ _____

How does your value for the pressure in the constriction compare to the measured values P_2 and P_4 ? You might consider how precisely you can determine both the calculated and measured pressures.

Next measure the pressure as for five different pump supply voltages to the pump. Be sure to let the flow stabilise before taking your readings. Complete the table below.

Voltage /V	P_1 /kPa	P_2 /kPa	P_3 /kPa	P_4 /kPa	Average of P_1 and P_3 /kPa	Average of P_2 and P_4 /kPa
5						
6						
8						
10						
12						

When you have finished, allow the reservoir to run empty and tilt the Venturi apparatus to empty water from it. Once the apparatus is empty of water remove the pressure tubes from the sensor by gently twisting the white plastic collars that connected the hoses to the sensor (leave the tubes connected to the underside of the Venturi apparatus). Empty as much water as you can from the apparatus and then **all of the water into the sink in the laboratory.**

Plot the two average pressures on the same graph, as a function of pump voltage. Do this by hand on this page, or, use JagFit (see back of manual) and attach your printed graphs to this page. Label axes correctly and include units. *Note, your tutor will account for fitting done by hand.*



Comment on your graph, is it consistent with what you expected to happen?

What can you conclude from this part of the experiment?

UCD Physics Laboratory: Investigation of Archimedes' Principle

Student Name: _____ Student Number: _____
Lab Partner Name: _____ Demonstrator Name _____
Lab Date/Time: _____

Introduction

All the technology we take for granted today, from electricity to motor cars, from television to X-rays, would not have been possible without a fundamental change, around the time of the Renaissance, to the way people questioned and reflected upon their world. Before this time, great **theories** existed about what made up our universe and the forces at play there. However, these theories were potentially flawed since they were never tested. As an example, it was accepted that heavy objects fall faster than light objects – a reasonable theory. However it wasn't until Galileo¹ performed an **experiment** and dropped two rocks from the top of the Leaning Tower of Pisa that the theory was shown to be false. Scientific knowledge has advanced since then precisely because of the cycle of **theory and experiment**. It is essential that every theory or hypothesis be tested in order to determine its veracity.

Physics is an experimental science. The theory that you study in lectures is derived from, and tested by experiment. Therefore in order to prove (or disprove!) the theories you have studied, you will perform various experiments in the practical laboratories.

First though, we have to think a little about what it means to say that your experiment confirms or rejects the theoretical hypothesis. Let's suppose you are measuring the acceleration due to gravity and you know that at sea level theory and previous experiments have measured a constant value of $g=9.81\text{m/s}^2$. Say your experiment gives a value of $g=10\text{ m/s}^2$. Would you claim the theory is wrong? Would you assume you had done the experiment incorrectly? Or might the two differing values be compatible?

What do you think?

¹ Actually, the story is probably apocryphal. However 11 years before Galileo was born, a similar experiment was published by Benedetti Giambattista in 1553.

Experimental Uncertainties

When you make a scientific measurement there is some ‘**true**’ value that you are trying to estimate and your equipment has some intrinsic **uncertainty**. Thus you can only estimate the ‘true’ value up to the uncertainty inherent within your method or your equipment. Conventionally you write down your measurement followed by the symbol \pm , followed by the uncertainty. A surveying company might report their results as 245 ± 5 km, 253 ± 1 km, 254.2 ± 0.1 km. You can interpret the second number as the ‘margin of error’ or the **uncertainty** on the measurement. If your uncertainties can be described using a Gaussian distribution, (which is true most of the time), then the true value lies within one or two units of uncertainty from the measured value. There is only a 5% chance that the true value is greater than two units of uncertainty away, and a 1% chance that it is greater than three units.

Errors may be divided into two classes, systematic and random. A **systematic error** is one which is constant throughout a set of readings. A **random error** is one which varies and which is equally likely to be positive or negative. Random errors are always present in an experiment and in the absence of systematic errors cause successive readings to spread about the true value of the quantity. If in addition a systematic error is present, the spread is not about the true value but about some displaced value.

Estimating the experimental uncertainty is at least as important as getting the central value, since it determines the range in which the truth lies.

Practical Example:

Now let’s put this to use by making some very simple measurements in the lab. We’re going to do about the simplest thing possible and measure the volume of a cylinder using three different techniques. You should compare these techniques and comment on your results.

Method 1: Using a ruler

The volume of a cylinder is given by $\pi r^2 h$ where r is the radius of the cylinder and h its height.

Measure and write down the height of the cylinder.
Don’t forget to include the uncertainty and the units.

$h = \quad \pm$

Measure and write down the diameter of the cylinder.

$d = \quad \pm$

Now calculate the radius.
(Think about what happens to the uncertainty)

$r = \quad \pm$

Calculate the radius squared – with it’s uncertainty!

$r^2 = \quad \pm$

One general way of determining the uncertainty in a quantity f calculated from others is to use the following method..

- From your measurements, calculate the final result. Call this f , your answer.
- Now move the value of the source up by its uncertainty. Recalculate the final result. Call this f^+ .
- The uncertainty on the final result is the difference in these values.

Finally work out the volume. Estimate how well you can determine the volume.

(Show your workings)

$$V = \pm$$

Method 2: Using a micrometer screw

This uses the same prescription. However your precision should be a lot better.

Measure and write down the height of the cylinder.
Don't forget to include the uncertainty and the units.

$$h = \pm$$

Measure and write down the diameter of the cylinder.

$$d = \pm$$

Now calculate the radius.

$$r = \pm$$

Calculate the radius squared, along with it's uncertainty

(Show your workings)

$$r^2 = \pm$$

Finally work out the volume.

(Show your workings)

$$V = \pm$$

Method 3: Using Archimedes' Principle

You've heard the story about the 'Eureka' moment when Archimedes dashed naked through the streets having realised that an object submerged in water will displace an equivalent volume of water. You will repeat his experiment (the displacement part at least) by immersing the cylinder in water and working out the volume of water displaced. You can find this volume by measuring the mass of water and noting that a volume of 0.001m^3 of water has a mass² of 1kg.

² In fact this is how the metric units are related. A litre of liquid is that quantity that fits into a cube of side 0.1m and a litre of water has a mass of 1kg.

Write down the mass of water displaced.

\pm

Calculate the volume of water displaced.

\pm

What is the volume of the cylinder?

\pm

Discussion and Conclusions.

Summarise your results, writing down the volume of the cylinder as found from each method.

\pm

\pm

\pm

Comment on how well they agree, taking account of the uncertainties.

Can you think of any systematic uncertainties that should be considered? Can you estimate their size?

Requote your results including the systematic uncertainties.

\pm \pm

\pm \pm

\pm \pm

What do you think the volume of the cylinder is? and why?

My best estimate of the volume is

\pm \pm

because _____

UCD Physics Laboratory: Investigation of Rotational Motion

Student Name: _____ **Student Number:** _____
Lab Partner Name: _____ **Demonstrator Name** _____
Lab Date/Time: _____

What should I expect in this experiment?

This experiment introduces you to some key concepts concerning rotational motion. These are: torque (τ), angular acceleration (α), angular velocity (ω), angular displacement (θ) and moment of inertia (I). They are the rotational analogues of force (F), acceleration (a), velocity (v), displacement (s) and mass (m), respectively.

Pre-lab assignment

What is the angular velocity of a spinning disk that completes 2 full revolutions in 10 seconds?

Introduction:

The equations of motion with constant acceleration are similar whether for linear or rotational motion:

Linear	Rotational	
$v_{average} = \frac{s_2 - s_1}{t_2 - t_1}$	$\omega_{average} = \frac{\theta_2 - \theta_1}{t_2 - t_1}$	Eq.1
$v_{average} = \frac{v_1 + v_2}{2}$	$\omega_{average} = \frac{\omega_1 + \omega_2}{2}$	Eq.2
$v_2 = v_1 + at$	$\omega_2 = \omega_1 + \alpha t$	Eq.3
$s_2 = v_1 t + \frac{at^2}{2}$	$q_2 = \omega_1 t + \frac{\alpha t^2}{2}$	Eq.4

Furthermore, just as a force is proportional to acceleration through the relationship $F=ma$, a net torque changes the state of a body's (rotational) motion by causing an angular acceleration.

$$\tau = I\alpha \quad \text{(Eq.5)}$$

The body's moment of inertia is a measure of resistance to this change in rotational motion, just as mass is a measure of a body's resistance to change in linear motion.

The equation $\tau = I\alpha$ is the rotational equivalent of Newton's 2nd law $F = ma$.

You will use two pieces of apparatus to investigate these equations. The first lets you apply and calculate torque, measure angular acceleration and determine an unknown moment of inertia, I of a pair of cylindrical weights located at the ends of a bar. The second apparatus lets you investigate how I depends on the distribution of mass about the axis of rotation and lets you determine the value of I , already measured in the first part, by a second method. You can then compare the results you obtained from the two methods.

Investigation 1: To measure the moment of inertia, I , from the torque and angular acceleration.

Place cylindrical masses on the bar at their furthest position from the axis of rotation. The bar is attached to an axle which is free to rotate. The masses attached to the line wound around this axle are allowed to fall, causing a torque about the axle



The value of the torque caused by the falling masses is $\tau = Fr$ where F is the weight of the mass attached to the string and r is the radius of the axle to which it is attached. Calculate the value of τ .

Mass, m attached to string (kg)	
Force, $F = m \cdot g$ (N)	
Radius, r of axle (m)	
Torque, $\tau = F \times r$ (Nm)	

In this session, you will calculate the angular velocity, ω , and the angular acceleration, α . Distinguish between these two underlined terms.

Wind the string attached to the mass around the axle until the mass is close to the pulley. Release it and measure the time for the bar to perform the first complete rotation, the second complete rotation, the third, fourth and fifth rotation. Estimate your experimental uncertainties.

Number of Rotations	θ (rad)	Time (s)
0	0	0
1		
2		
3		
4		
5		

Since you have the angular distance travelled in a given time you can use Eq. 4 to find the angular acceleration α . Explain how you can do this and find a value for α .

$\alpha =$

Using Eq.1, calculate the average velocity, $\omega_{average}$, during each rotation and fill in the table below.

If angular acceleration is constant, then $\omega_{average}$ is equal to the instantaneous velocity at the time half-way between the start and the end of a rotation, t_{mid} . Can you understand this? Explain.

Enter the values in the table below and **make a plot** of $\omega_{average}$ on the y-axis against t_{mid} on the x-axis.

Number of Rotation	$\omega_{average}$ (rad / s)	t_{mid} (s)
1		
2		
3		
4		
5		

Since this graph gives the instantaneous velocity at a given time, Eq. 3 can be used to find the angular acceleration, α .

What value do you get for α ?

Now you know τ and α , so work out I from Eq. 5.

Create your graph of $\omega_{average}$ on the y-axis against t_{mid} on the x-axis.

Do the following plot by hand on this page, or, use JagFit (see back of manual) and attach your printed graph to this page. Important: take care to label axes correctly and include units. *Note, your tutor will account for fitting where done by hand.*



Investigation 2: To determine how the moment of inertia, I , depends on the distribution of mass in a body.

Take the metal bar on the bench and roll it between your hands. Now hold it in the middle and rotate it about its centre so that the ends are moving most. Which is easier? Which way does the bar have a higher value of I ?

Attach the weights and the bar to the rotational apparatus known as a **torsion axle**. This consists of a vertical axle connected to a spring which opposes any departure from the angle of rotational equilibrium.

Note: The apparatus is delicate. So as not to damage the spring, please keep the rod to within half a rotation from equilibrium.



When you rotate the bar, the spring causes a torque about the axis of rotation which acts to restore the bar to the equilibrium angle. Usually the bar overshoots, causing an oscillation to occur. This is exactly analogous to the way a mass on a linear spring undergoes simple harmonic motion. The period of the oscillations, T , is determined by the restoring torque in the spring, D , and the moment of inertia, I , of the object rotating, in this case the bar and cylindrical weights. They are related by:

$$T = 2\pi\sqrt{\frac{I}{D}}$$

The value of D is written on each torsion axle. Note it here.

To investigate the influence of mass distribution vary the position of the cylinders along the torsion bar, measure the period of oscillation, T , and use the equation above to calculate the moment of inertia, I for the combined system of cylinders plus rod. (To improve the precision with which you measure T take the average over 10 oscillations.)

r – Position of the cylinders along rod (m)	T – Period of oscillation (s)	I for the combined system of cylinder + bar (kgm^2)	I for the cylinders (kgm^2)
0.05			
0.10			
0.15			
0.20			
0.25			

Just as you can simply add two masses together to get the total mass (e.g. if the mass of a cylinder is 0.24kg and the mass of a bar is 0.2kg, then the mass of cylinder plus bar is 0.44kg) you can also add moments of inertia together. Given that the moment of inertia of the bar is 0.00414 kgm^2 , will let you fill in the fourth column in the table above.

Plot the value of I_{cylinder} against the position r .

Plot the value of I_{cylinder} against the position r^2 .

What do you conclude?

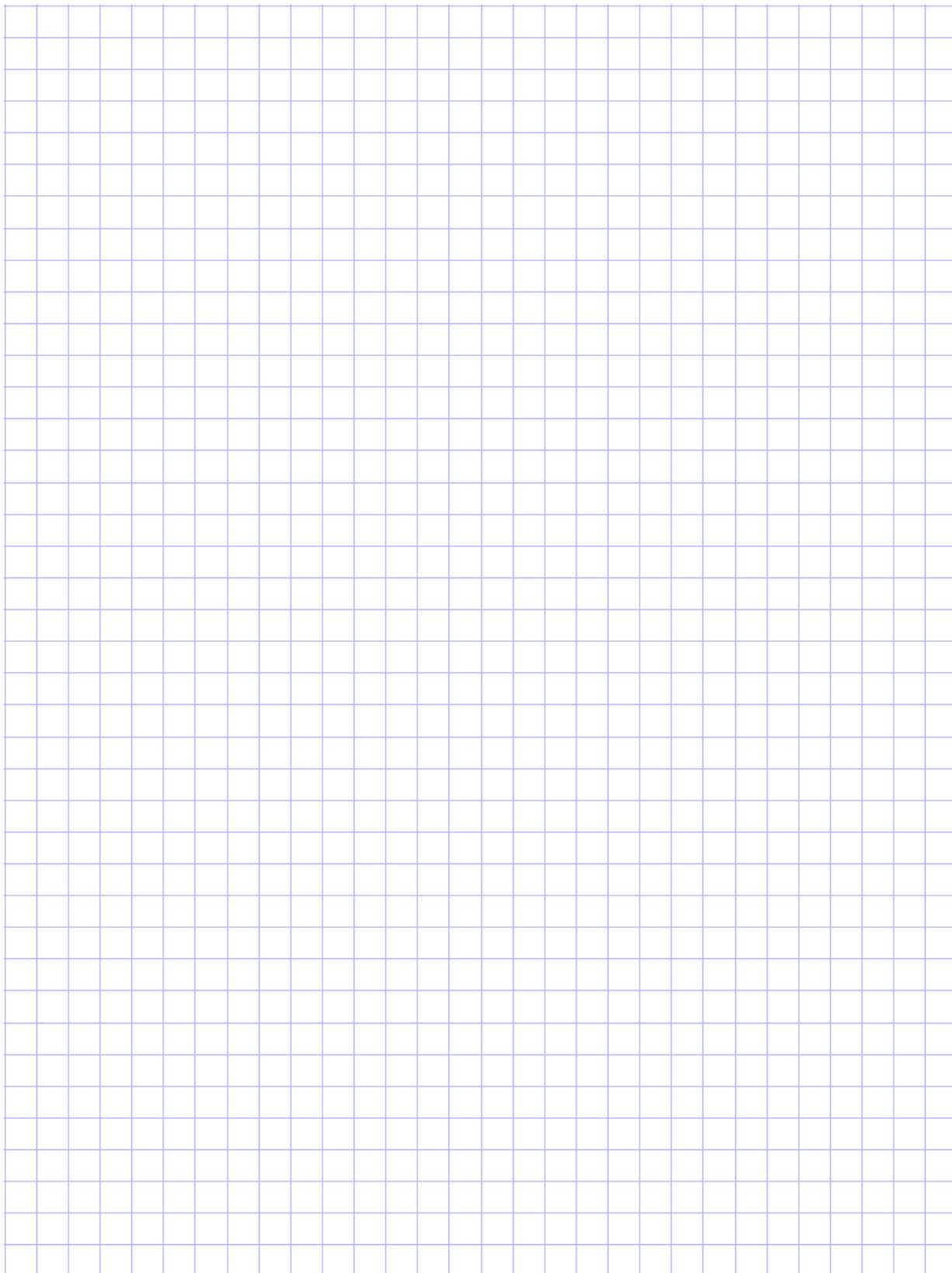
Create a graph of I_{cylinder} against the position, r .

Do the following plot by hand on this page, or, use JagFit (see back of manual) and attach your printed graph to this page. Important: take care to label axes correctly and include units. *Note, your tutor will account for fitting where done by hand.*



Create a graph of I_{cylinder} against the position, r^2 .

Do the following plot by hand on this page, or, use JagFit (see back of manual) and attach your printed graph to this page. Important: take care to label axes correctly and include units. *Note, your tutor will account for fitting where done by hand.*



The last measurement in the table above, with $r = 0.25\text{m}$, returns the bar + cylinders system to the orientation used in your first investigation. You have thus measured the moment of inertia of the bar + cylinder system in two independent ways. Write down the two answers that you got.

/ from investigation 1:

/ from investigation 2:

How do the two values compare? Which is more precise?

Graphing

Many of the experiments in the 1st Year laboratory involve the plotting of a graph. Graphs are very important in Physics as they provide a rich display of the results obtained in an experiment. One third of the human brain is devoted to images, and so we are well optimised to interact with graphs rather than with tables of numbers.

Plotting graphs by hand:

- (1) *Scale:* It is important to choose the scales so as to make full use of the squared page. The scale divisions should be chosen for convenience; that is, one unit is either 1, 2 or 5 times a power of ten e.g. 0.5, 5, 100 etc., but never 3, 7, 9 etc.
- (2) *Marking the points:* Readings should be indicated on the graph by a ringed dot \otimes and drawn with pencil, so that it is possible to erase and correct any unsatisfactory data.
- (3) *Joining the points:* In the case of a straight line which indicates a direct proportion between the variables, the ruler is positioned so that the line drawn will pass through as many points as possible. Those points which do not lie on the line should be equally distributed on both sides of the line. A point which lies away from this line can be regarded as 'doubtful' and a recheck made on the readings. In the case of a curve, the individual experimental points are not joined with straight lines but a smooth curve is drawn through them so that as many as possible lie on the curve.
- (4) *Units:* The graph is drawn on squared page. Each graph should carry title at the top e.g. Time squared vs. Length. The axes should be labelled with the name and units of the quantities involved.
- (5) In the case of a straight-line graph, the equation of the line representing the relationship between the quantities x and y may be expressed in the form

$$y = mx + c$$

where m is the slope of the line and c the intercept on the y -axis. The slope may be positive or negative. Many experiments require an accurate reading of the slope of a line.

Using JagFit

In the examples above we have somewhat causally referred to the '**best fit**' through the data. What we mean is, the curve which comes closest to the data points having due regard for the experimental uncertainties.

We can judge this really quite well by eye, but so isn't quantitative or reproducible between people necessarily, and so doing this manually isn't always the best way.

We can determine a straight line fit to data that varies due to random fluctuations using so-called 'least square fitting', but this requires a calculator/computer and sufficiently large data sets. At least 10 measurements are required to be usefully quantitative in this way, and more typically more than 30 measurements are needed.

A computer can make a difference where data sets are large enough then, and a plotting program called Jagfit is installed on the computers. Jagfit is freely available for download from this address:

<http://www.southalabama.edu/physics/software/software.htm>



If you are to use it, then double-click on the JagFit icon to start the program. The working of JagFit is fairly intuitive. Enter your data in the columns on the left.

- Under Graph, select the columns to graph, and the name for the axes.
- Under Error Method, you can include uncertainties on the points.
- Under Tools, you can fit the data using a function as defined under Fitting Function. Normally you will just perform a linear fit.

Three of the experiments in this manual were initially developed by the Physics Education Group, CASTeL, Dublin City University.